

DARK MATTER MINI HALOS FROM PRIMORDIAL MAGNETIC FIELDS

Phys. Rev. Lett. 131, 231002

Pranjal Ralegankar

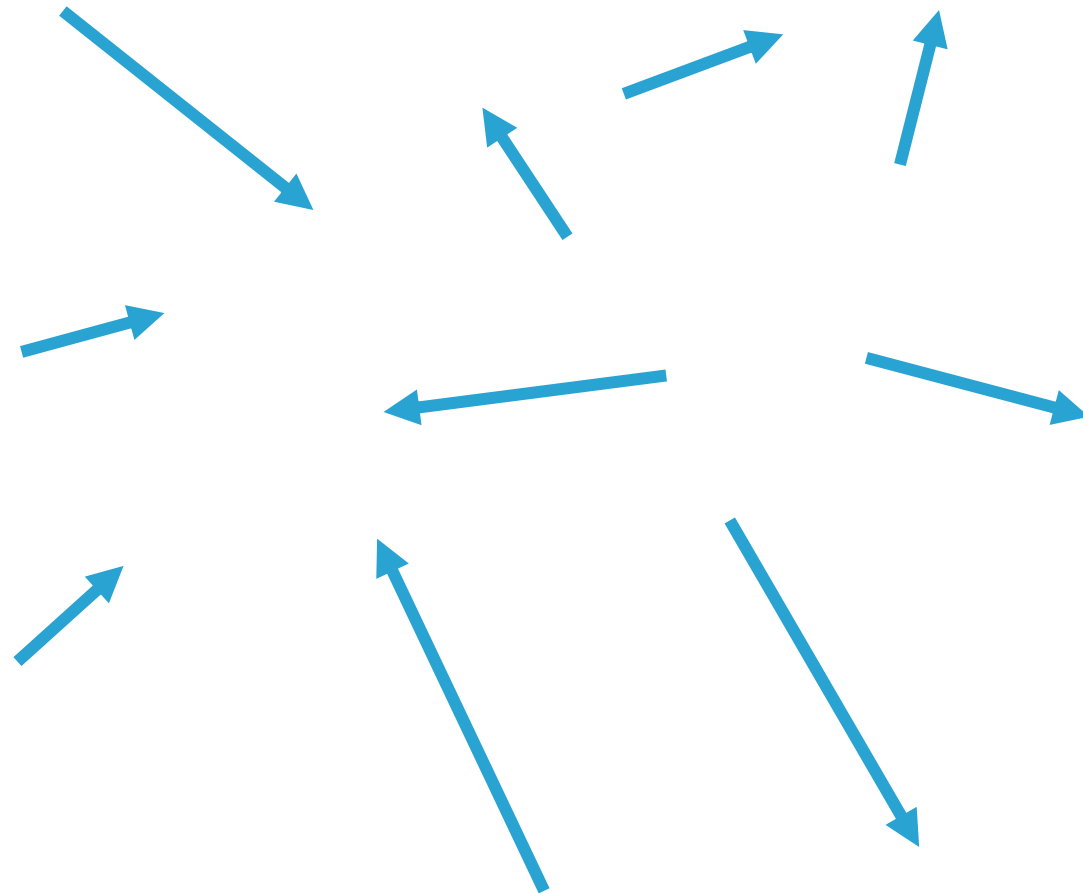
Postdoctoral scientist, SISSA

Image source: Pauline Voß for Quanta Magazine

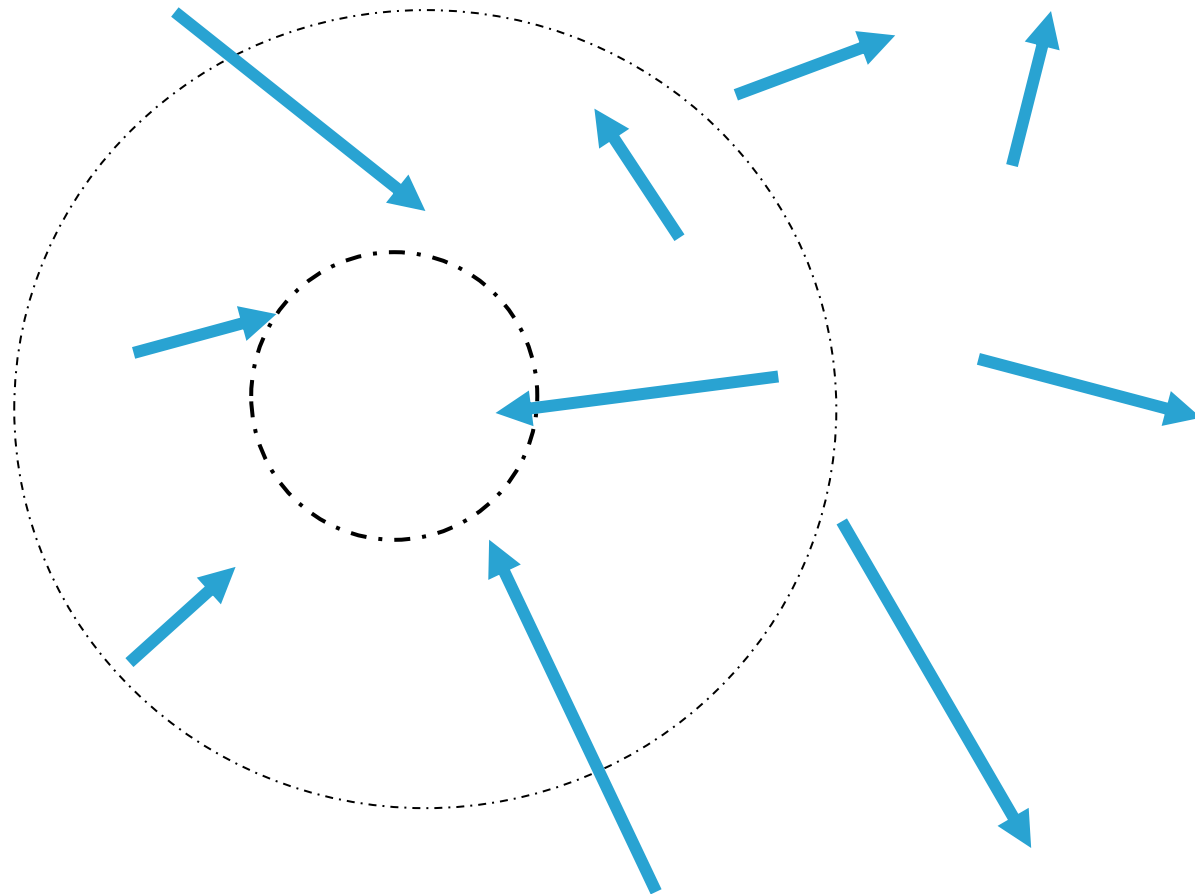
PRIMORDIAL MAGNETIC FIELDS ENHANCE DENSITY PERTURBATIONS



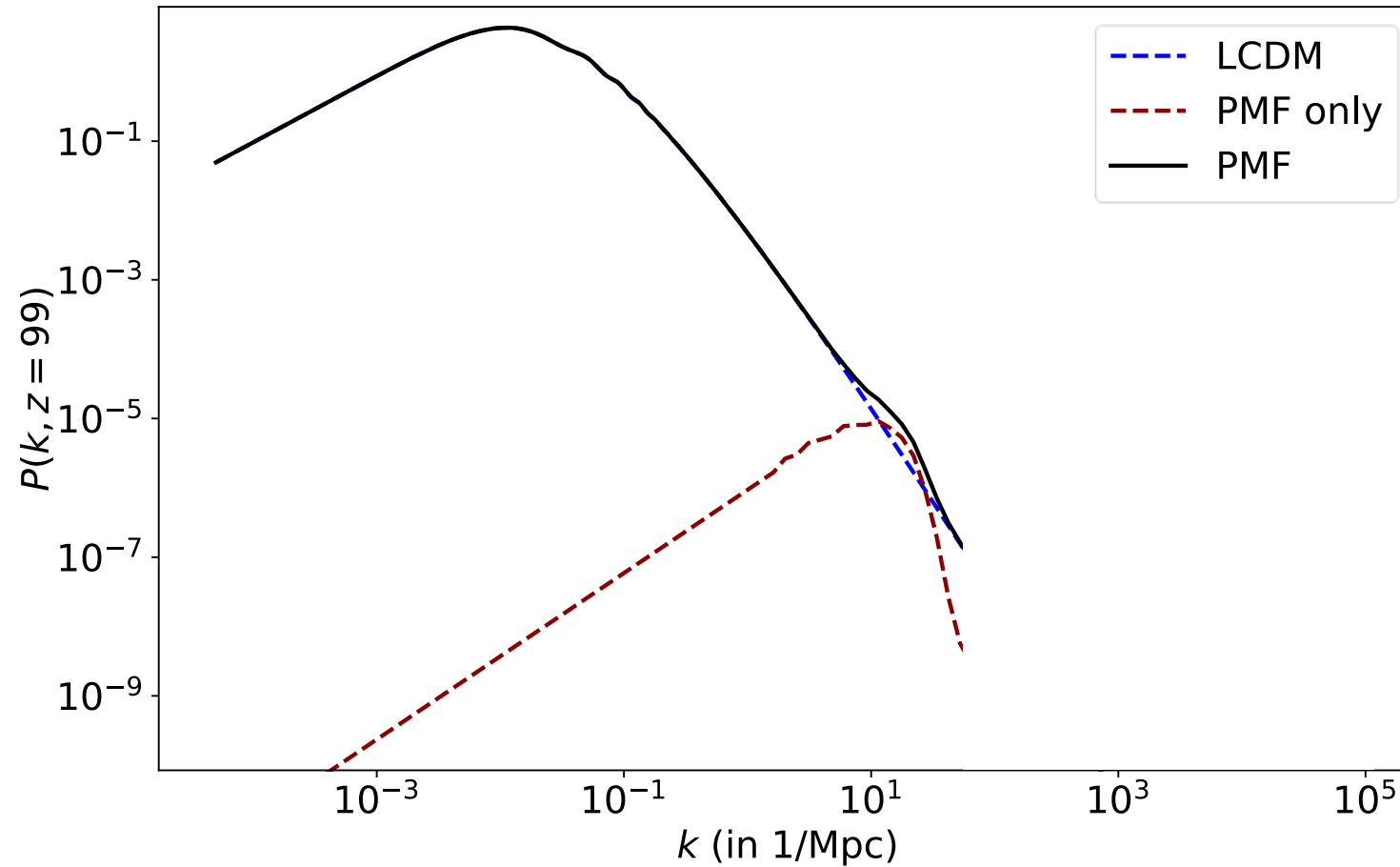
PRIMORDIAL MAGNETIC FIELDS ENHANCE DENSITY PERTURBATIONS



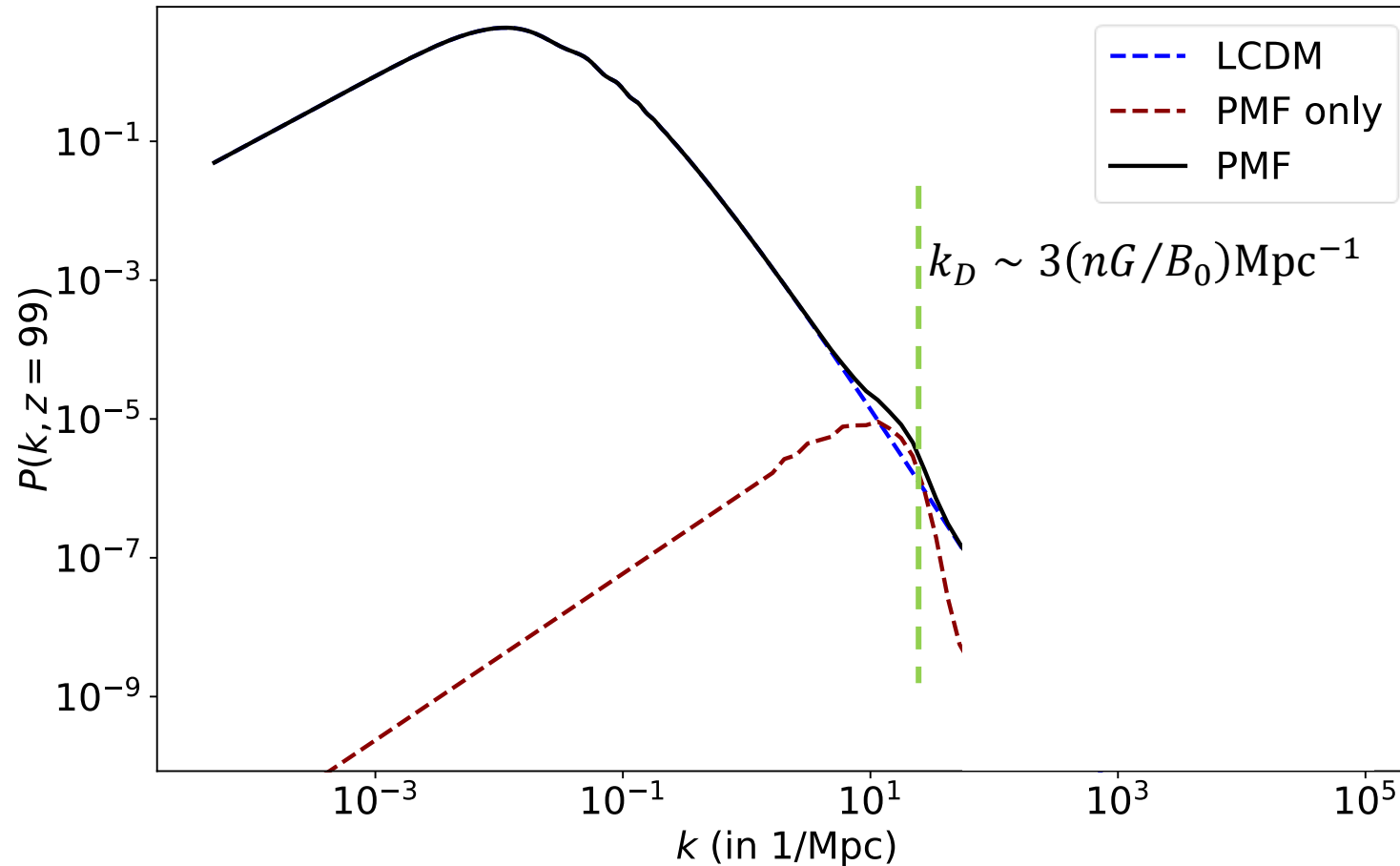
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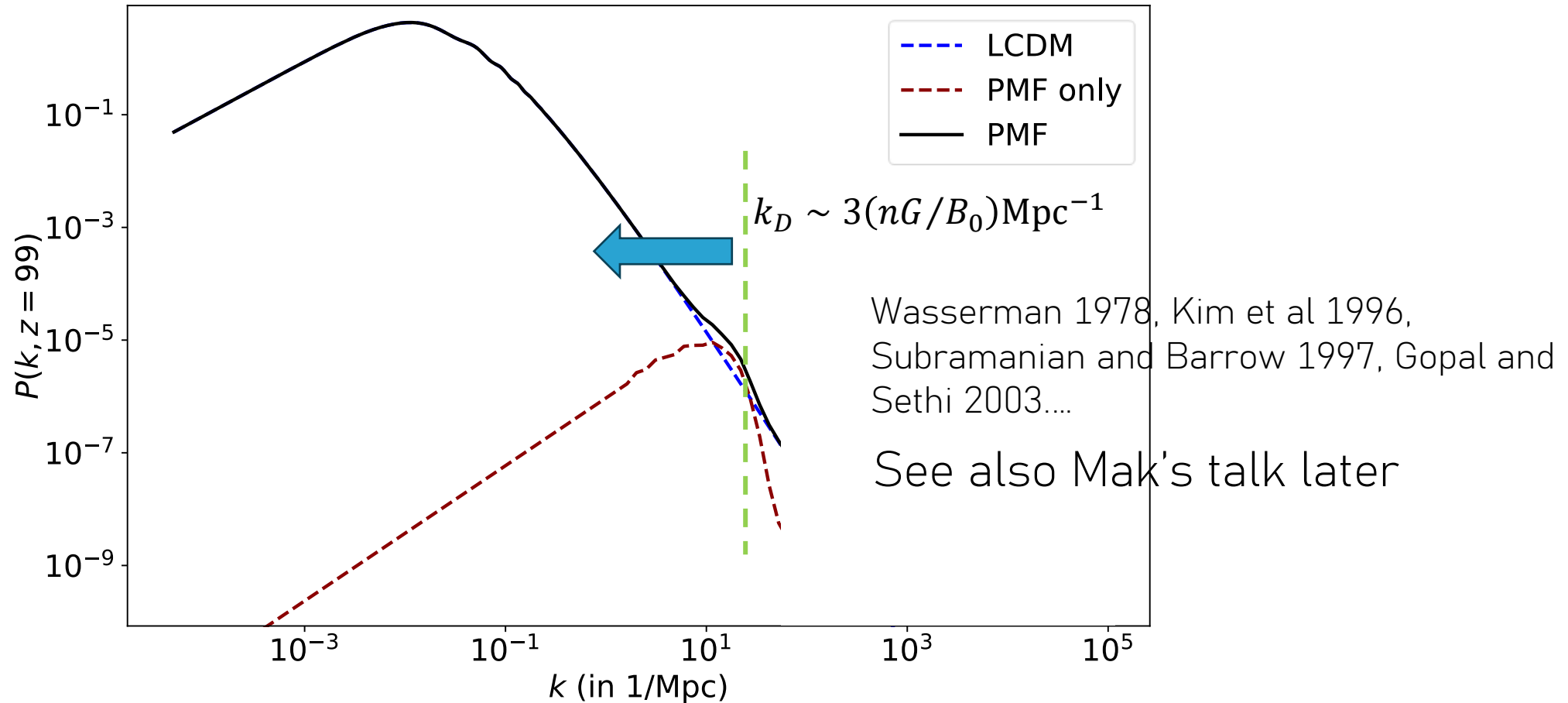
PRIMORDIAL MAGNETIC FIELDS ENHANCE POWER SPECTRUM ON SMALL SCALES



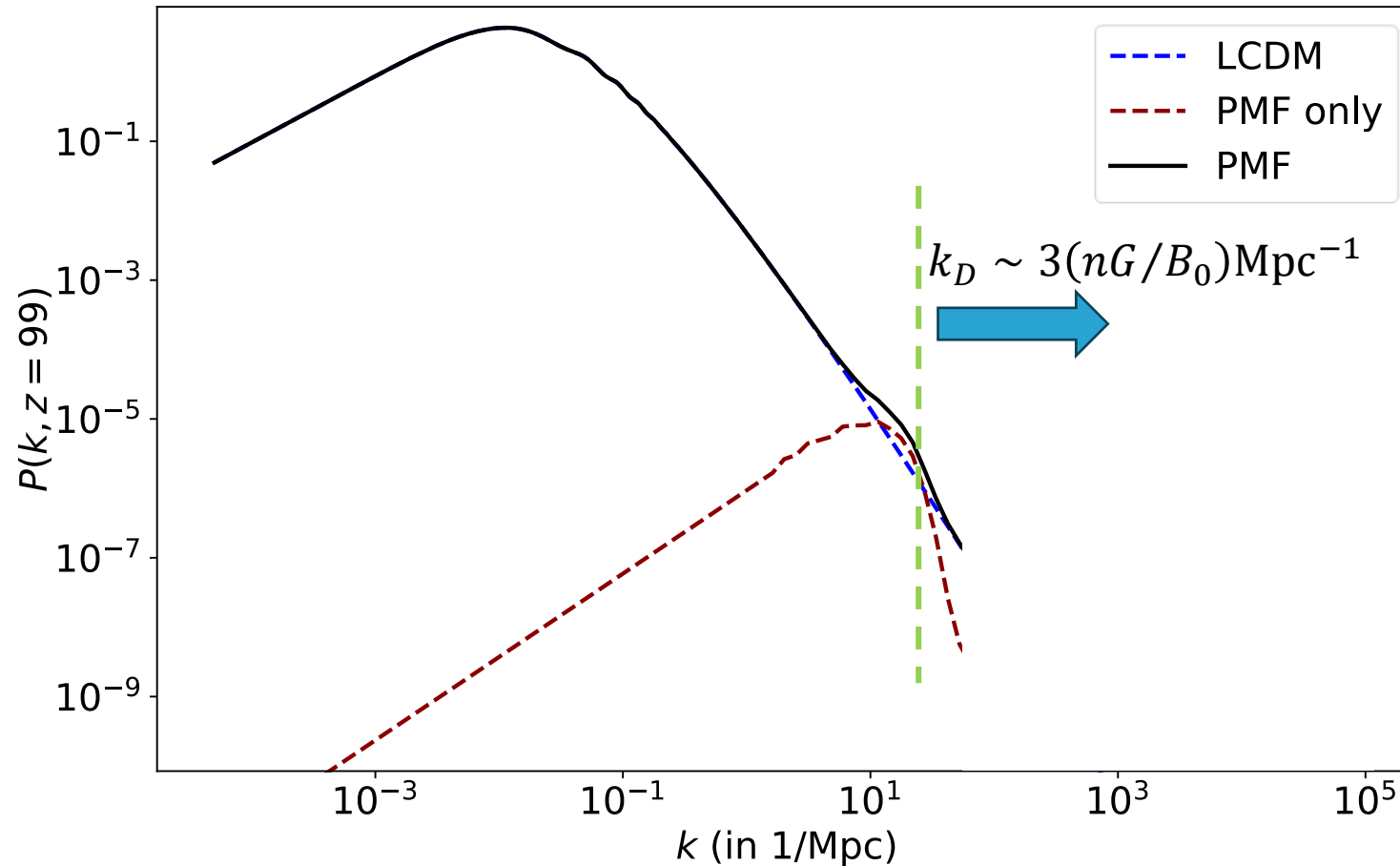
BACKREACTION FROM BARYONS SUPPRESSES BARYON DENSITY PERTURBATIONS BELOW MAGNETIC DAMPING (JEANS) SCALE



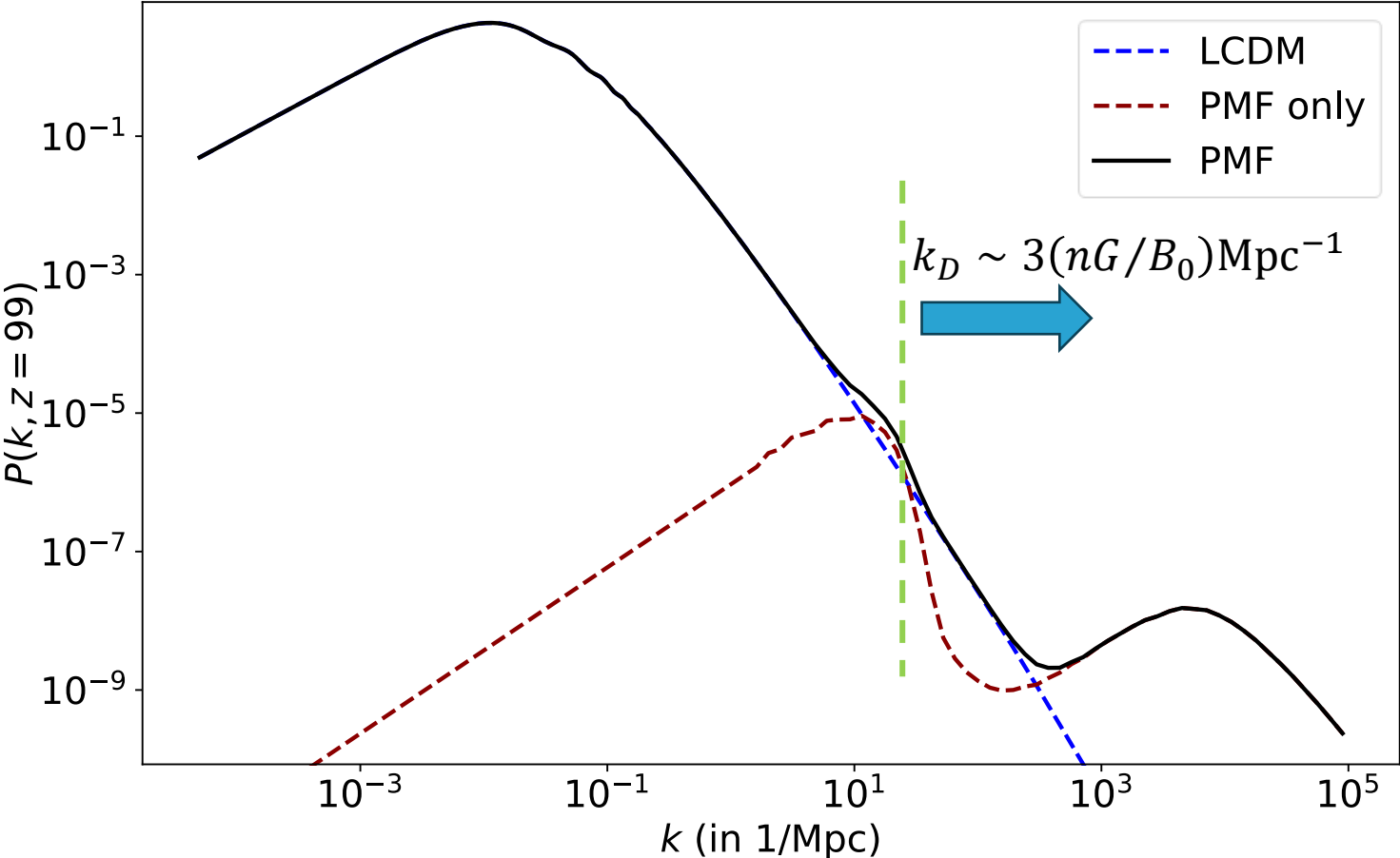
EARLIER WORKS FOCUSED ON SCALES BELOW MAGNETIC DAMPING (JEANS) SCALE



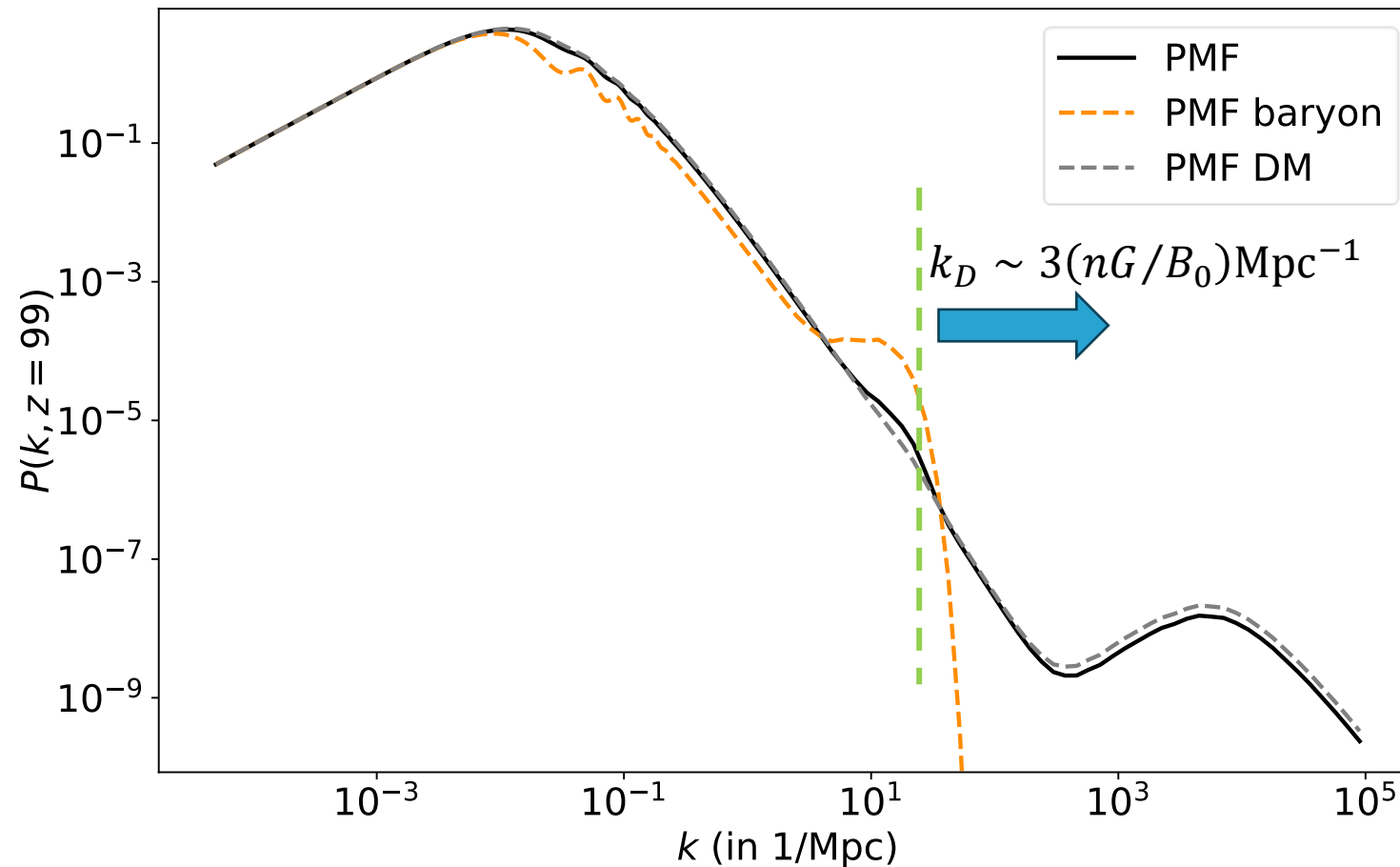
MY STUDY FOCUSES ON SCALES BELOW MAGNETIC DAMPING (JEANS) SCALE



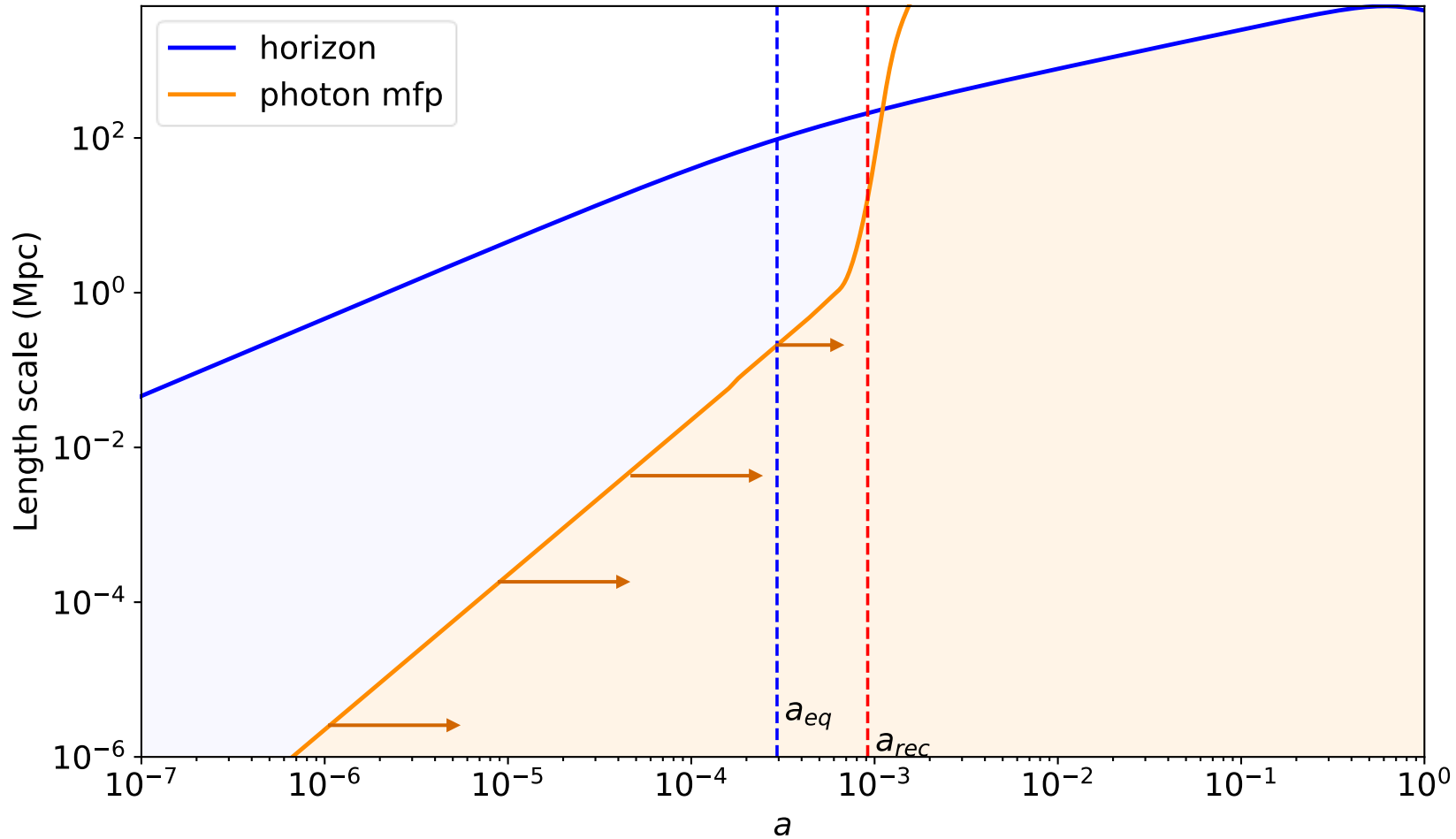
FINDING: HIGHLY ENHANCED POWER SPECTRUM BELOW JEANS SCALE



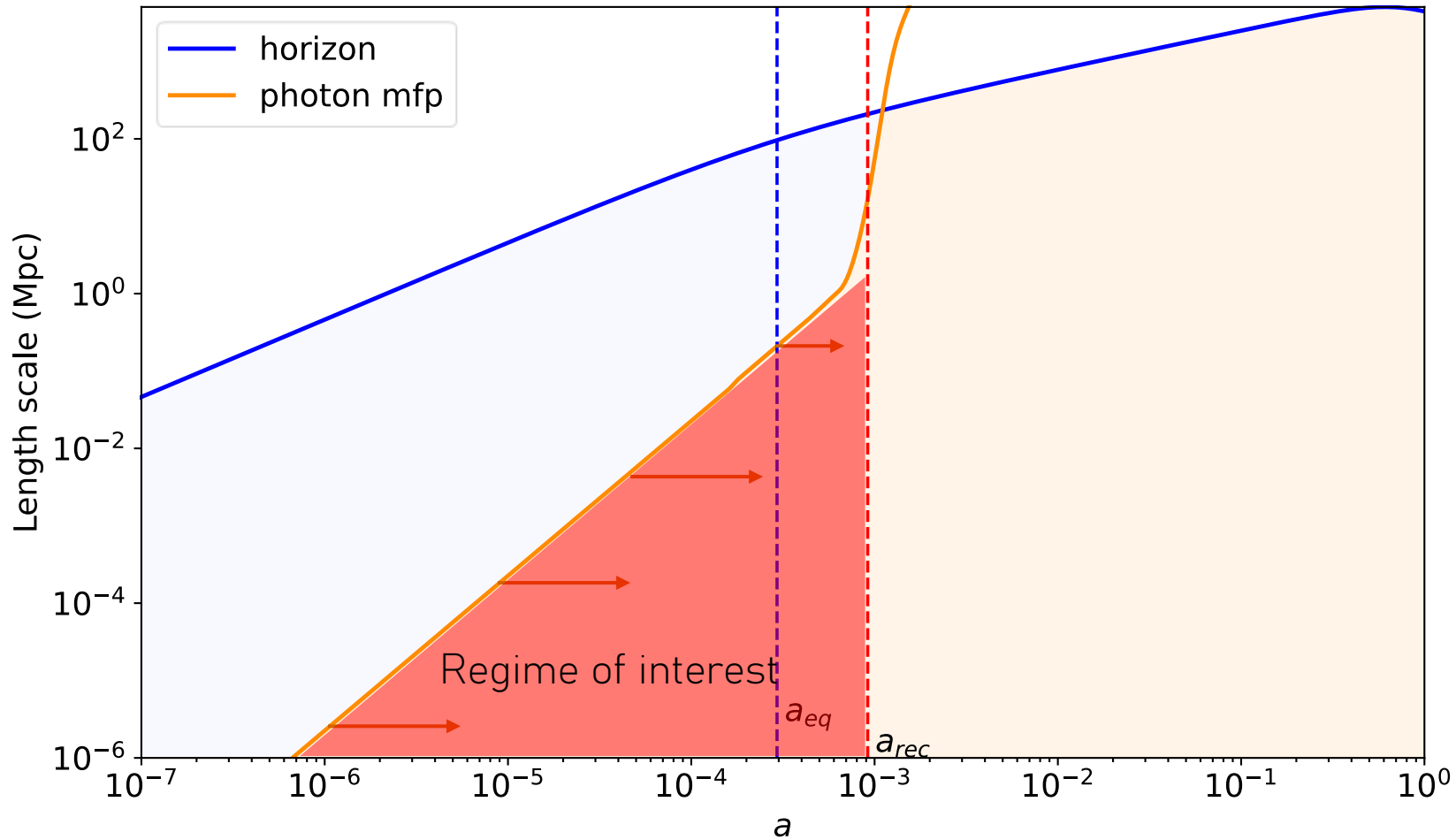
FINDING: BARYON PERTURBATION SUPPRESSED BELOW JEANS SCALE BUT NOT DARK MATTER!



SCALES OF INTEREST: PRE-RECOMBINATION AND SCALES SMALLER THAN PHOTON MFP



SCALES OF INTEREST: PRE-RECOMBINATION AND SCALES SMALLER THAN PHOTON MFP



IDEAL MHD IN PHOTON DRAG REGIME:

IDEAL MHD IN PHOTON DRAG REGIME: LAMINAR FLOW IN BARYONS

$$\frac{\partial \vec{v}_b}{\partial t} + (H + \alpha) \vec{v}_b + \frac{(\vec{v}_b \cdot \nabla) \vec{v}_b}{a} = \frac{(\nabla \times \vec{B}) \times \vec{B}}{4\pi a \rho_b} - \frac{c_b^2 \nabla \delta_b}{a} - \frac{\nabla \phi}{a}$$

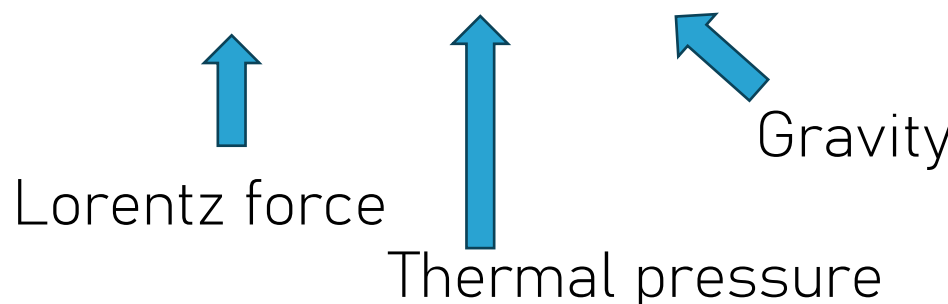
IDEAL MHD IN PHOTON DRAG REGIME: LAMINAR FLOW IN BARYONS

$$\frac{\partial \vec{v}_b}{\partial t} + (H + \alpha) \vec{v}_b = \frac{(\nabla \times \vec{B}) \times \vec{B}}{4\pi a \rho_b} - \frac{c_b^2 \nabla \delta_b}{a} - \frac{\nabla \phi}{a}$$

Abel and Jedamzik 2010,
Campanelli 2013,
Jedamzik and Saveliev 2018

IDEAL MHD IN PHOTON DRAG REGIME: KEY FORCES

$$\frac{\partial \vec{v}_b}{\partial t} + (H + \alpha)\vec{v}_b = \frac{(\nabla \times \vec{B}) \times \vec{B}}{4\pi a \rho_b} - \frac{c_b^2 \nabla \delta_b}{a} - \frac{\nabla \phi}{a}$$


Lorentz force Thermal pressure Gravity

IDEAL MHD IN PHOTON DRAG REGIME: LARGE LORENTZ FORCE LIMIT

$$(H + \alpha)\vec{v}_b \approx \frac{(\nabla \times \vec{B}) \times \vec{B}}{4\pi\alpha\rho_b}$$

IDEAL MHD IN PHOTON DRAG REGIME: LARGE LORENTZ FORCE LIMIT

$$(H + \alpha)\vec{v}_b \approx \frac{(\nabla \times \vec{B}) \times \vec{B}}{4\pi a \rho_b}$$

$$\frac{\partial (a^2 \vec{B})}{\partial t} = \frac{\nabla \times (\vec{v}_b \times a^2 \vec{B})}{a}$$

IDEAL MHD IN PHOTON DRAG REGIME: MAGNETIC DAMPING SCALE

$$(H + \alpha)\vec{v}_b \approx \frac{(\nabla \times \vec{B}) \times \vec{B}}{4\pi a \rho_b}$$

$$\frac{\partial (a^2 \vec{B})}{\partial t} = \frac{\nabla \times (\vec{v}_b \times a^2 \vec{B})}{a}$$

$$P_B(k, t) = P_B(k, t_I) e^{-\frac{k^2}{k_D^2}}$$

$$k_D^{-1}(a) \sim \tau v_b$$

Campanelli 2013

IDEAL MHD IN PHOTON DRAG REGIME: MAGNETIC DAMPING SCALE

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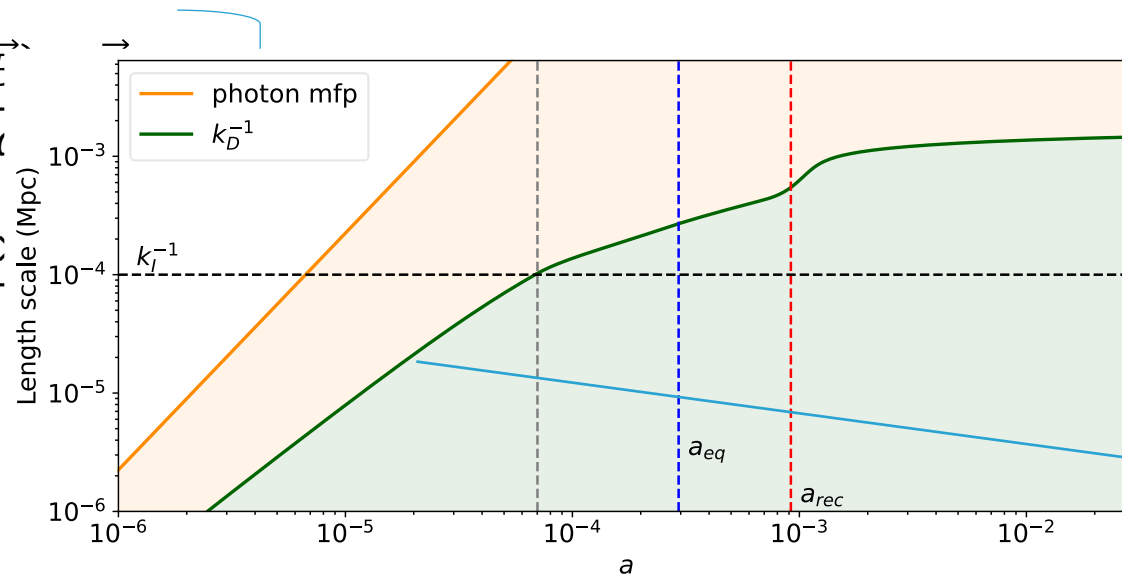
Campanelli 2013

ASSUMED
 B_0 Gaussian

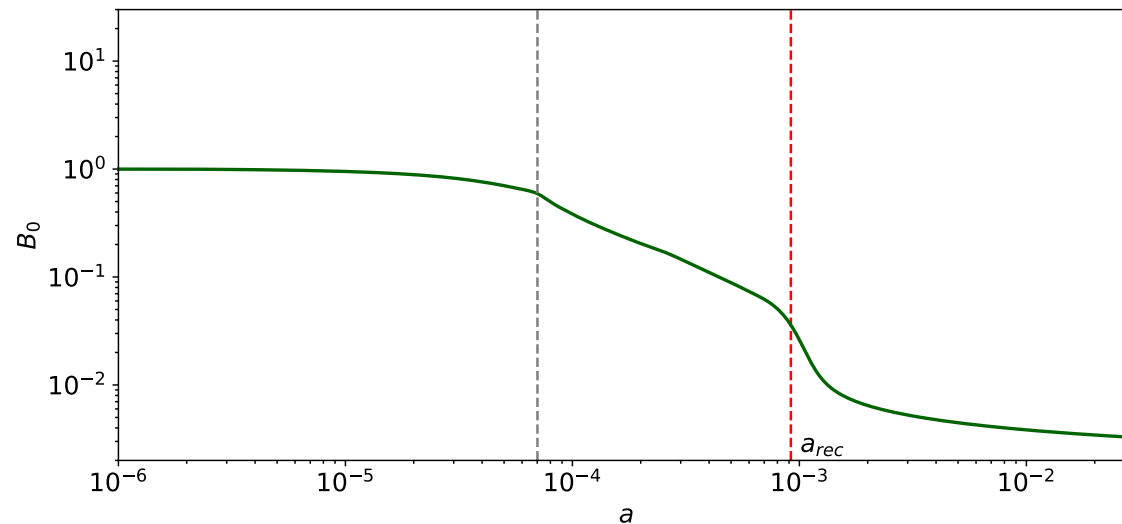
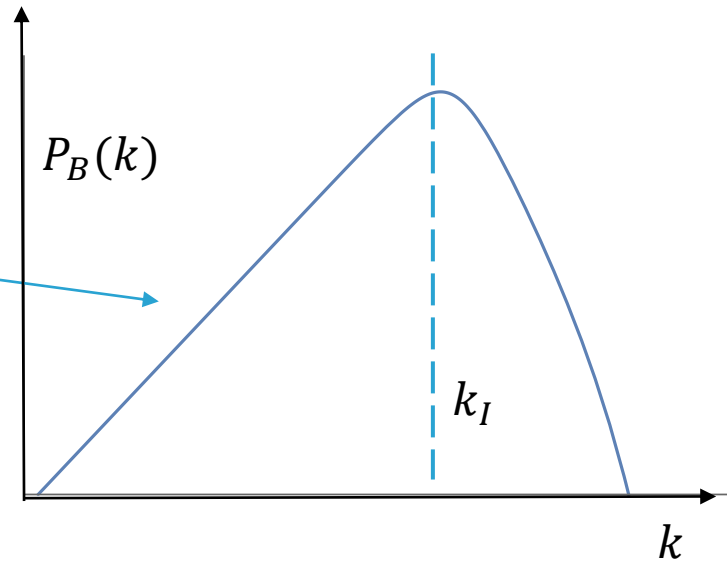
IDEAL MHD IN PHOTON DRAG REGIME: DAMPING SCALE GROWS WITH TIME

$$(H + \alpha)\vec{v}_b \approx \frac{(\nabla \times \vec{E})}{4\pi\epsilon}$$

$$\frac{\partial (a^2 \vec{B})}{\partial t} = \frac{\nabla \times (\vec{v}_b \cdot \vec{B})}{a}$$



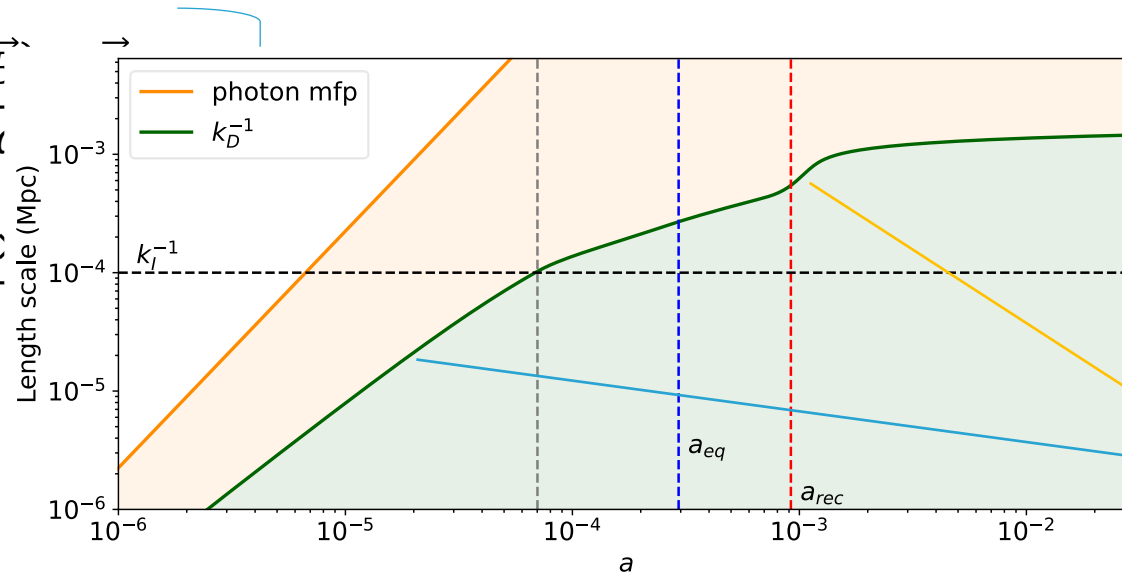
$$k_D^{-1}(a) \sim \tau v_A$$



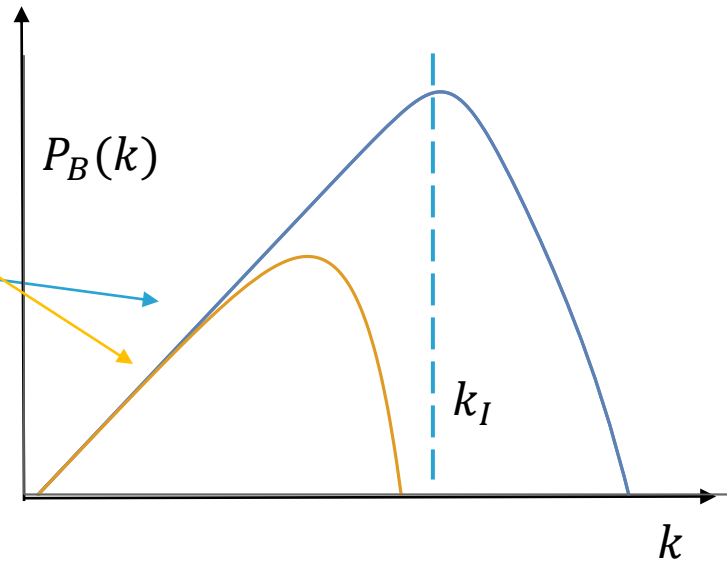
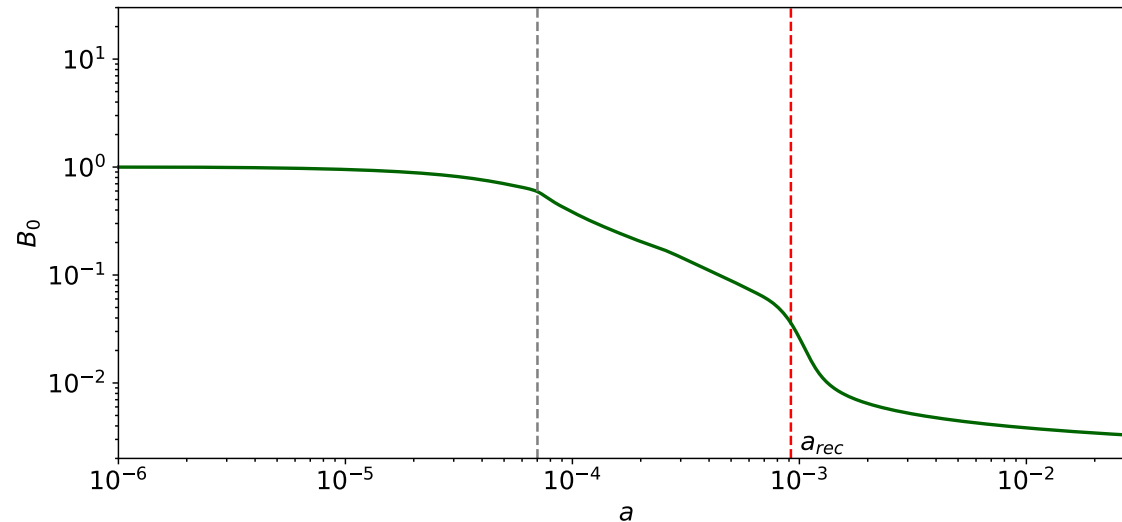
IDEAL MHD IN PHOTON DRAG REGIME: DAMPING SCALE GROWS WITH TIME

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$$\frac{\partial (a^2 \vec{B})}{\partial t} = \frac{\nabla \times (\vec{v}_b \cdot \dots)}{a}$$



$$k_D^{-1}(a) \sim \tau v_A$$



SOLVING DENSITY PERTURBATION EQUATIONS

$$L_B = \frac{(\nabla \times \vec{B}) \times \vec{B}}{4\pi a \rho_b}$$

$$\frac{\partial \vec{v}_b}{\partial t} + (H + \alpha) \vec{v}_b = L_B - \frac{c_b^2 \nabla \delta_b}{a} - \frac{\nabla \phi}{a}$$

$$\frac{\partial \delta_b}{\partial t} = -\frac{\nabla \cdot \vec{v}_b}{a}$$

$$\nabla^2 \phi = \frac{a^2}{2M_{Pl}^2} (\rho_b \delta_b + \rho_{DM} \delta_{DM})$$

$$\frac{\partial^2 \delta_{DM}}{\partial a^2} + \left[\frac{\partial \ln(a^2 H)}{\partial \ln a} + 1 \right] \frac{\partial \delta_{DM}}{a \partial a} = \frac{\nabla^2 \phi}{(a^2 H)^2}$$

SOLVING DENSITY PERTURBATION EQUATIONS

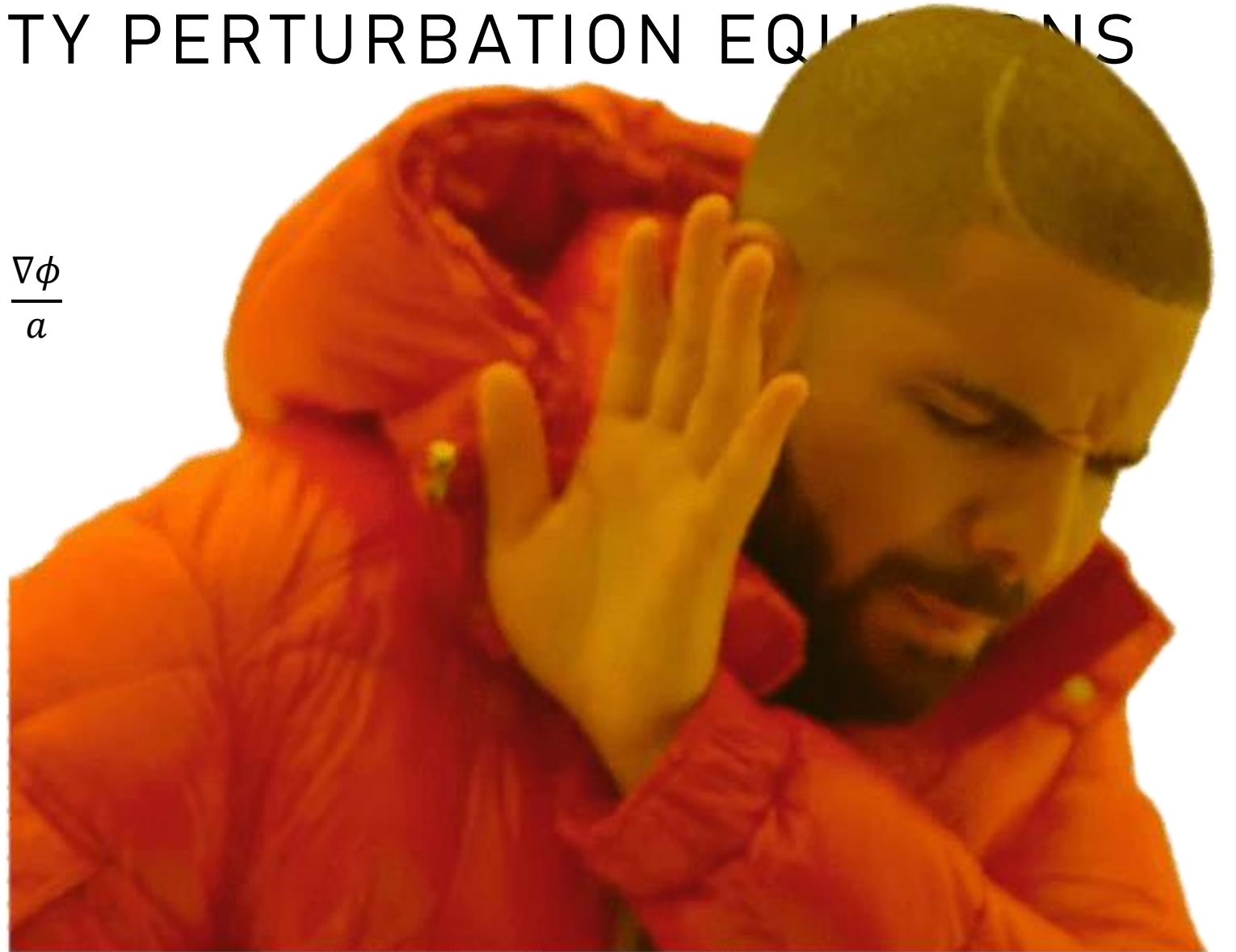
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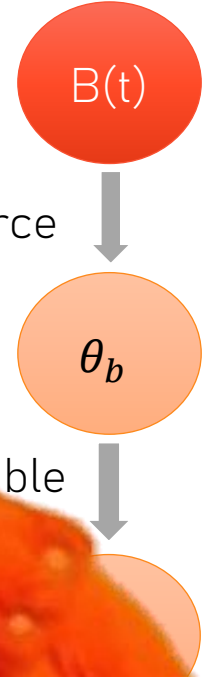
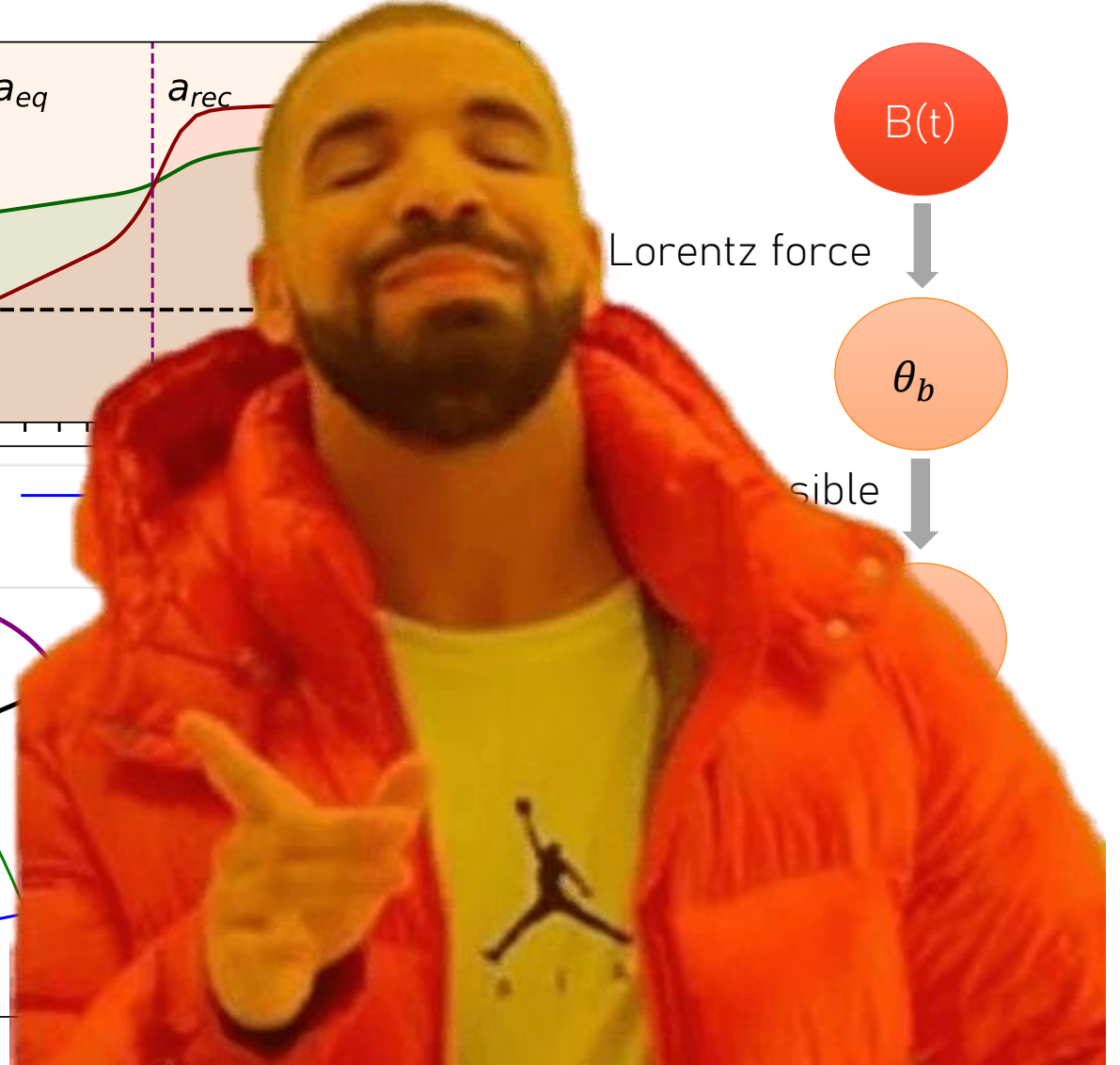
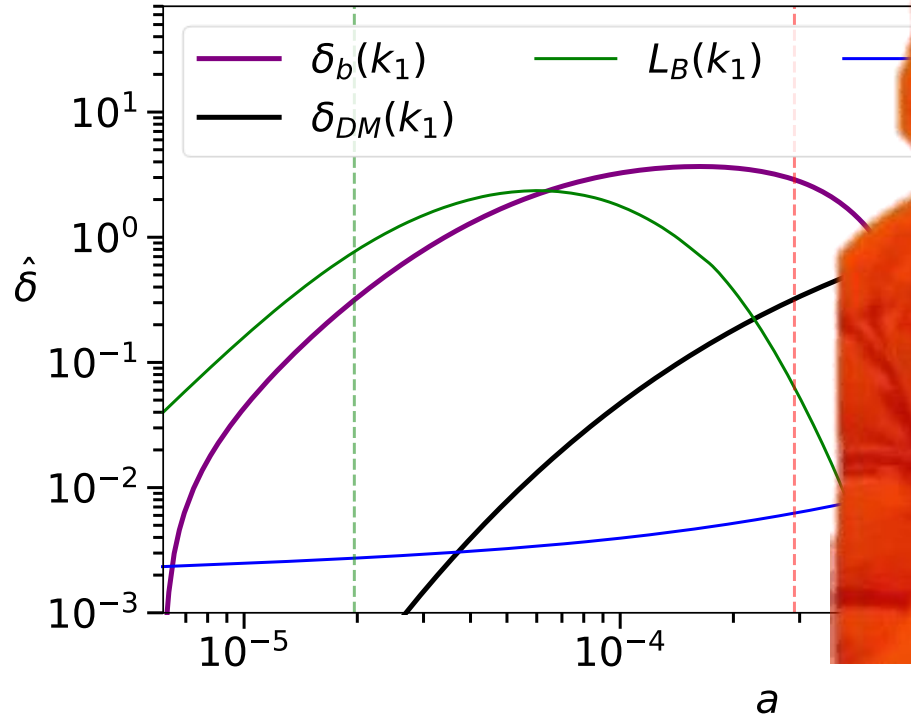
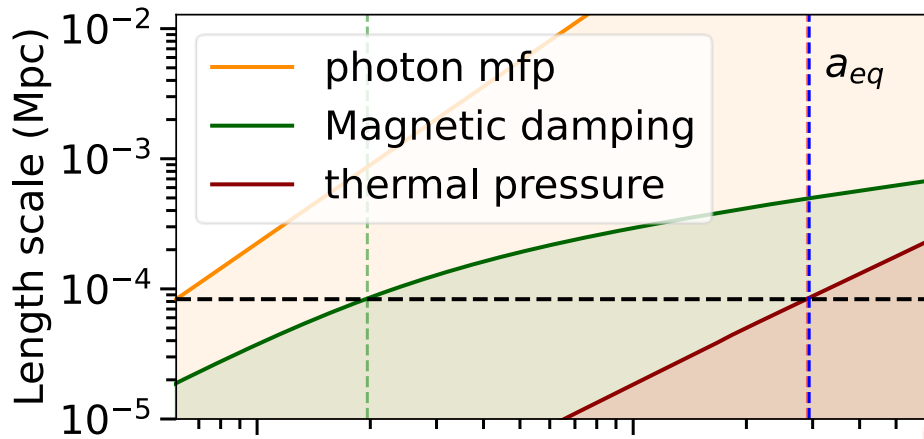
$$\nabla^2 \phi = \frac{a^2}{2M_{Pl}^2} (\rho_b \delta_b + \rho_{DM} \delta_{DM})$$

$$\frac{\partial^2 \delta_{DM}}{\partial a^2} + \left[\frac{\partial \ln(a^2 H)}{\partial \ln a} + 1 \right] \frac{\partial \delta_{DM}}{a \partial a} =$$



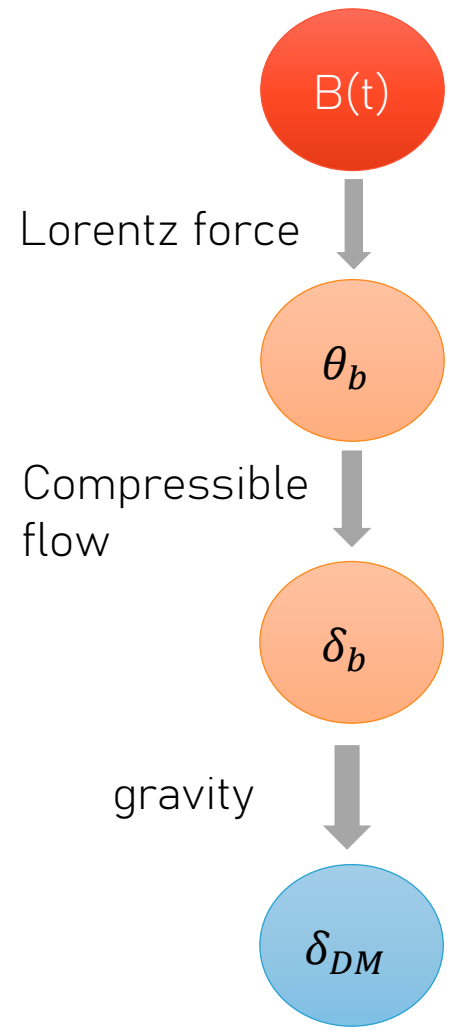
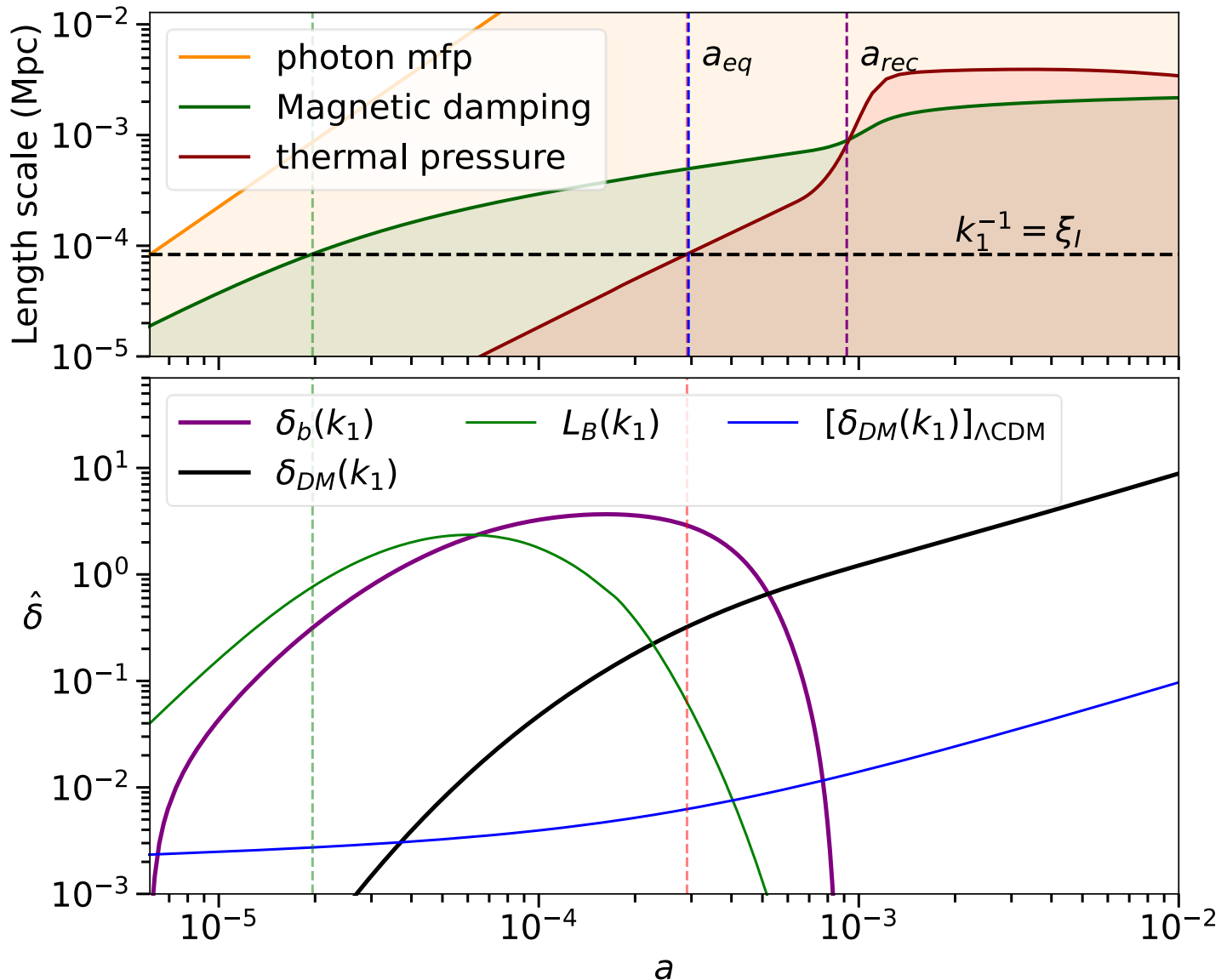
PERTURBATION EVOLUTION PLOT

$B_I = 5 \text{ nG}$



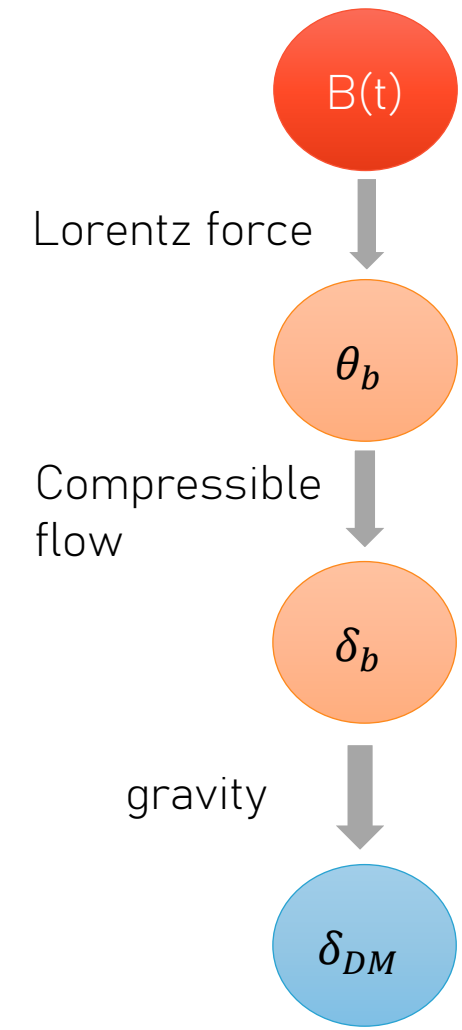
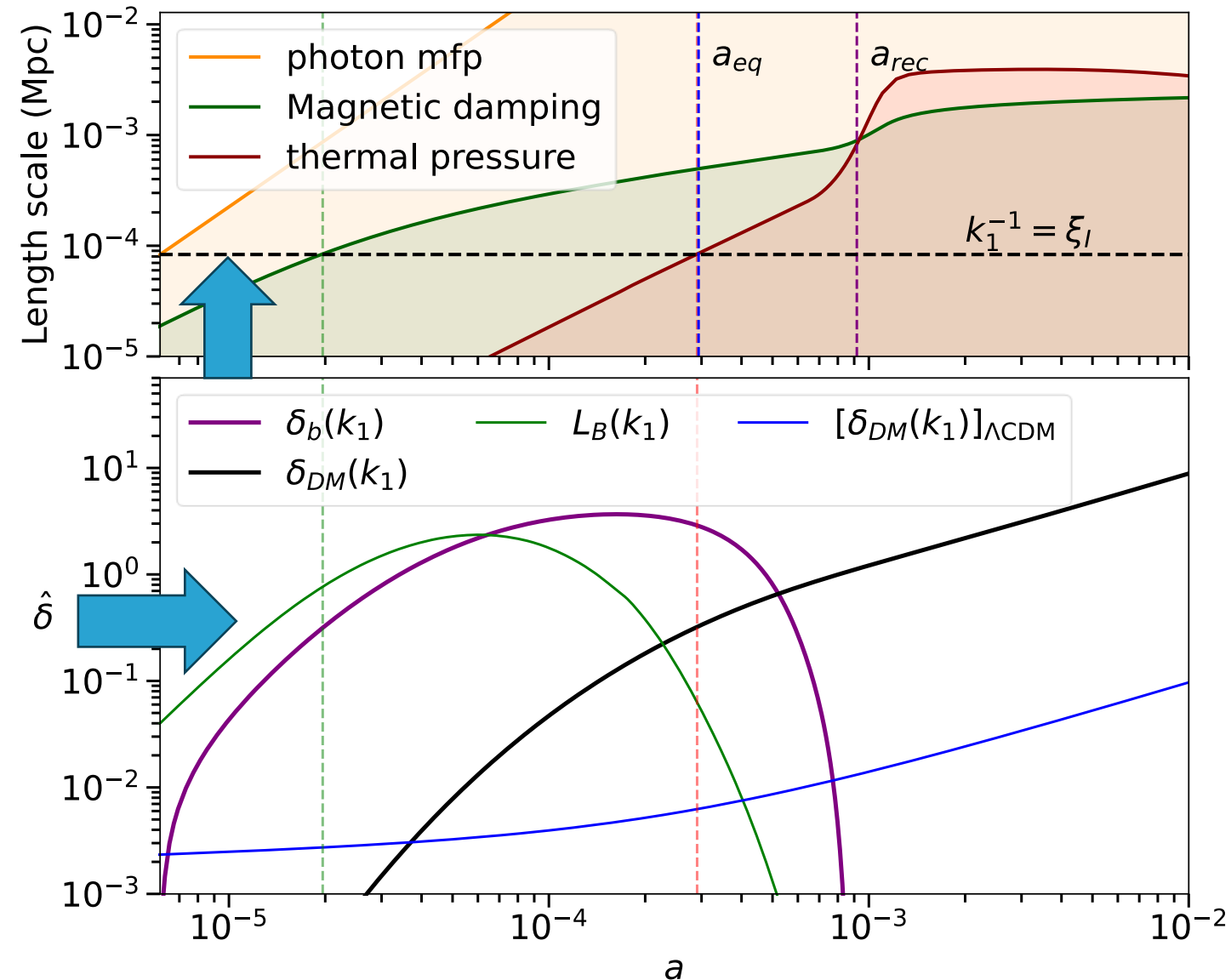
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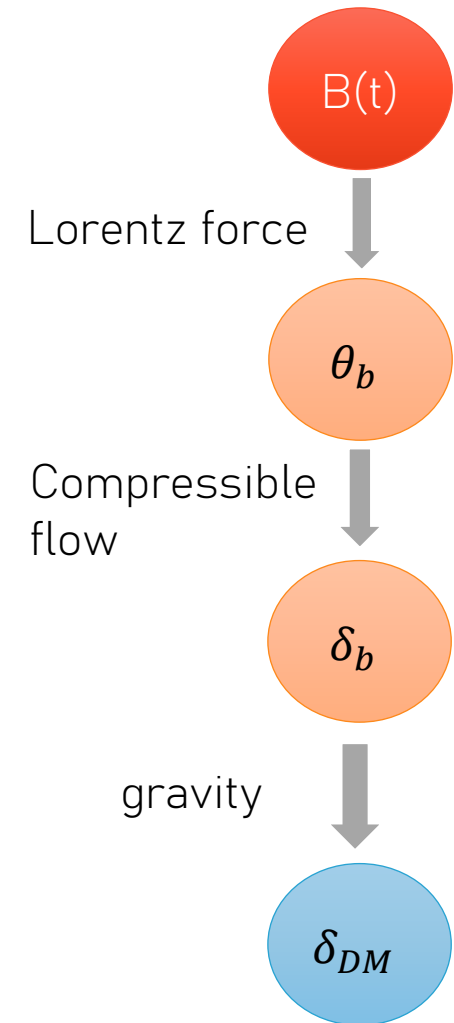
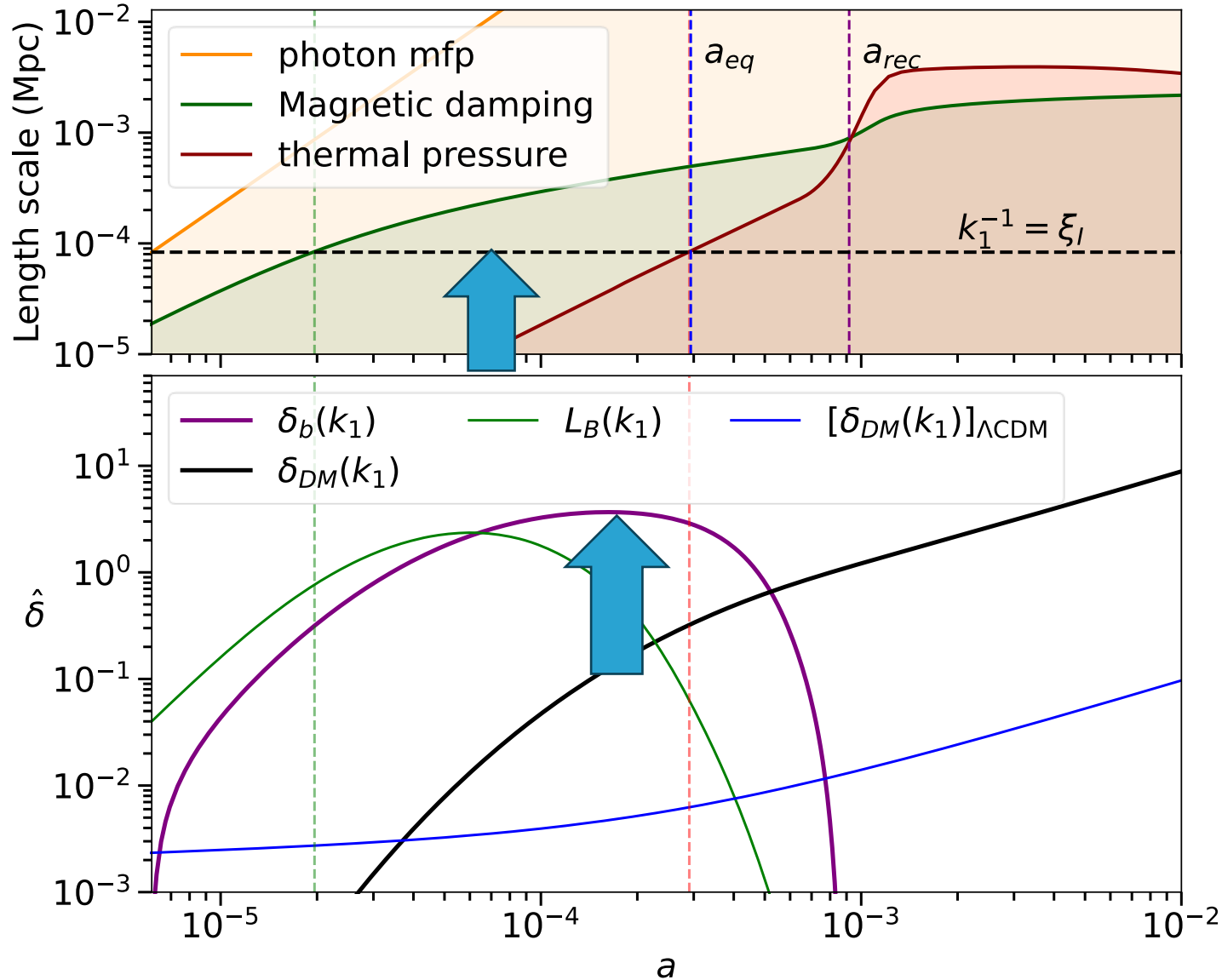
LORENTZ FORCE ENHANCES BARYON PERTURBATIONS FOR MODES OUTSIDE k_D^{-1}

$B_I = 5 \text{ nG}$



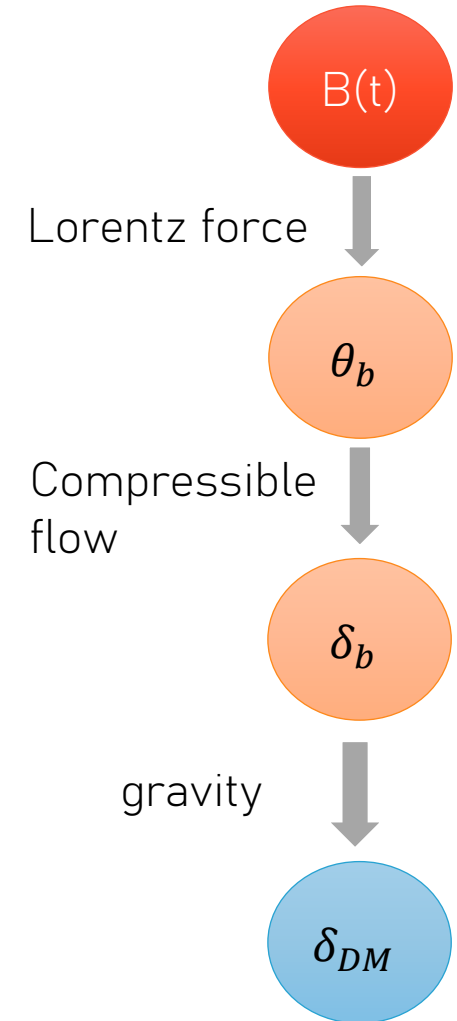
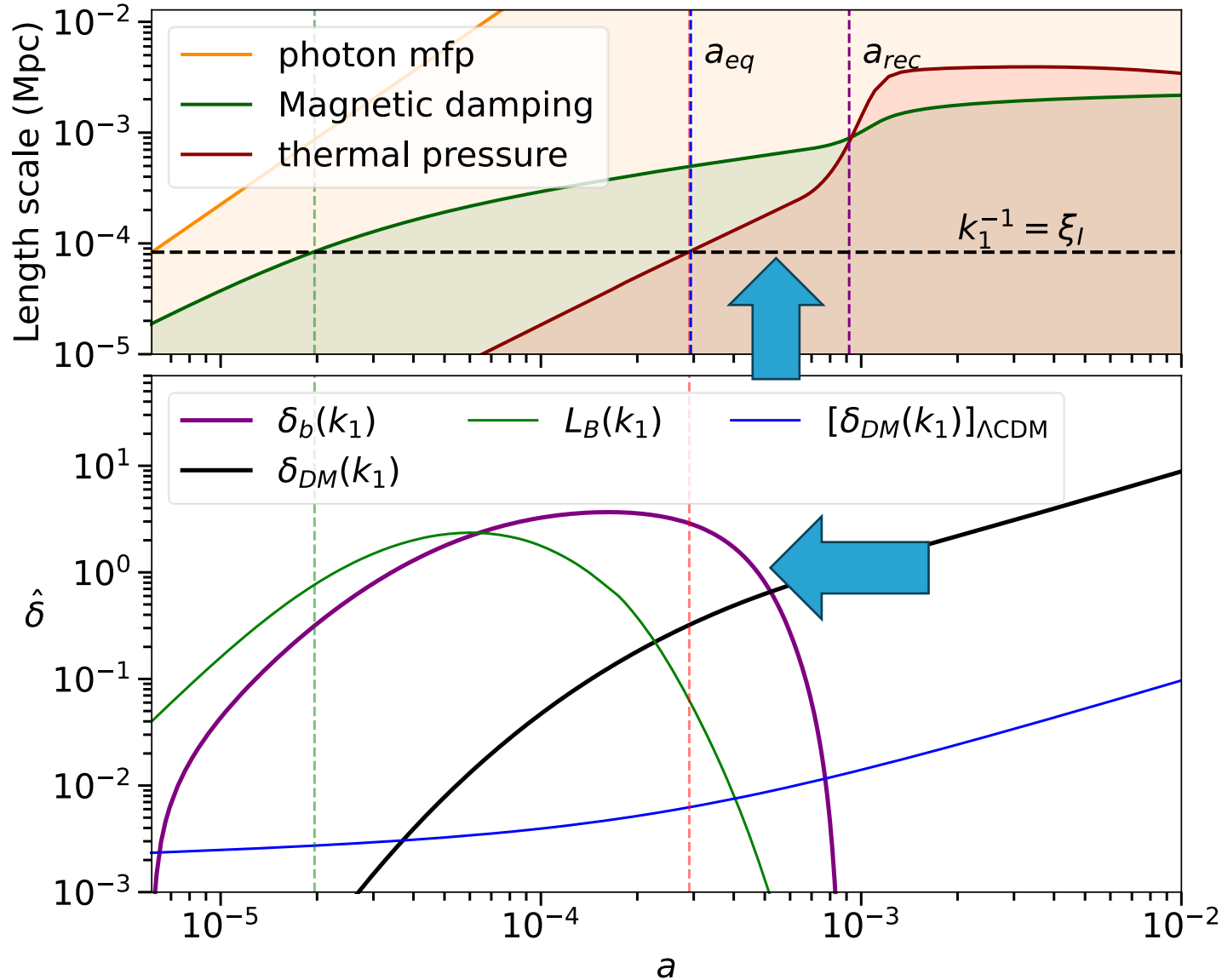
BARYON PERTURBATIONS ASYMPTOTE ONCE MODE ENTERS k_D^{-1}

$B_I = 5 \text{ nG}$



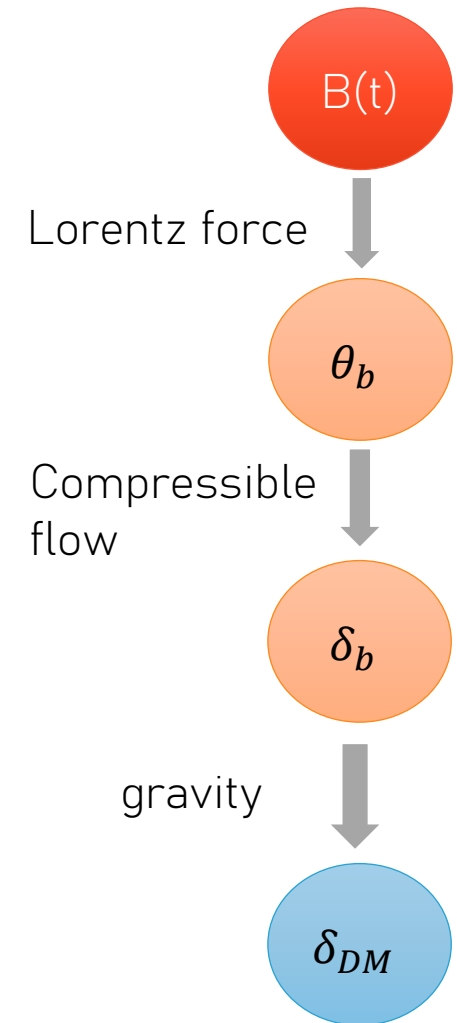
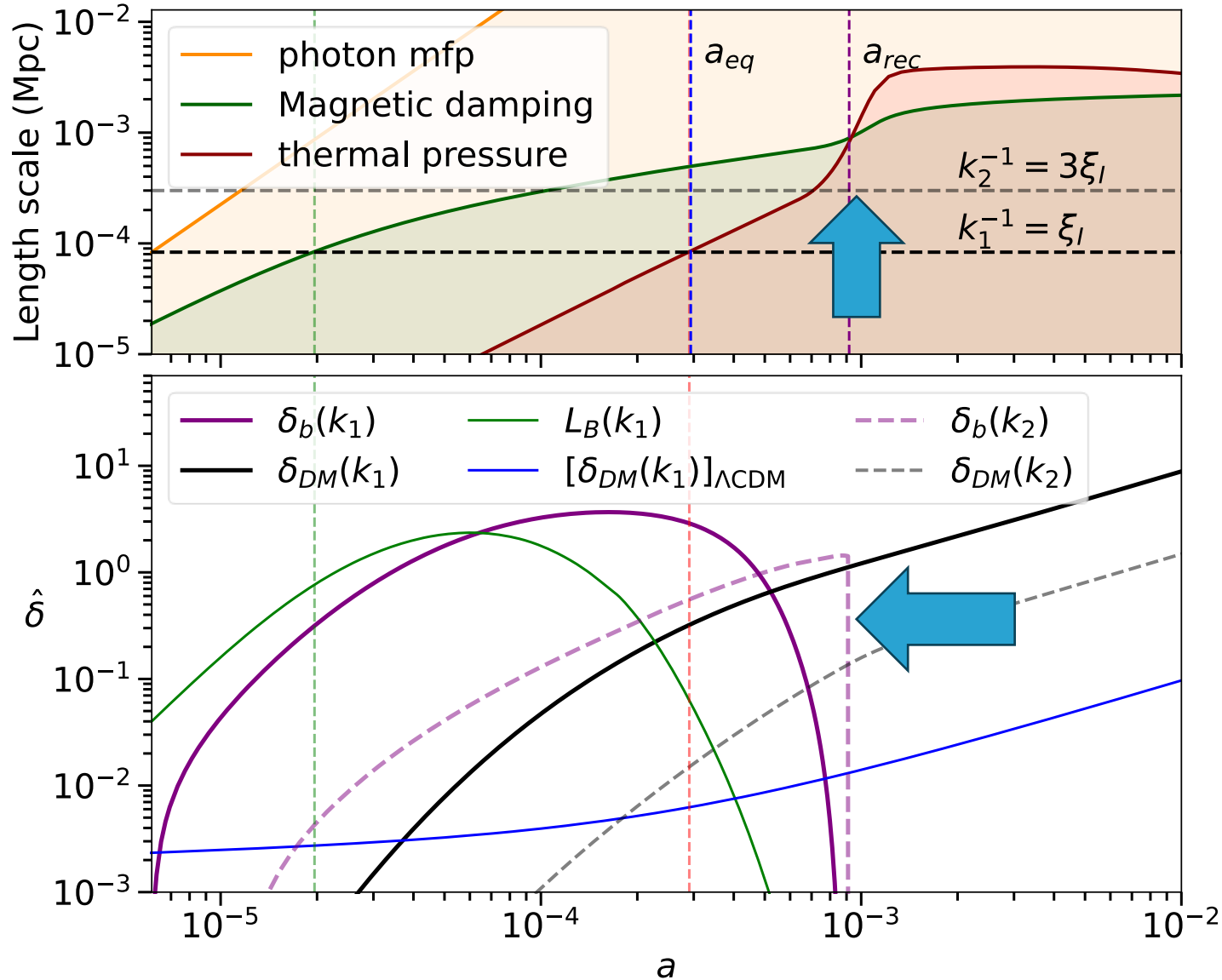
BARYON PERTURBATIONS DAMPED BY THERMAL PRESSURE

$B_I = 5 \text{ nG}$



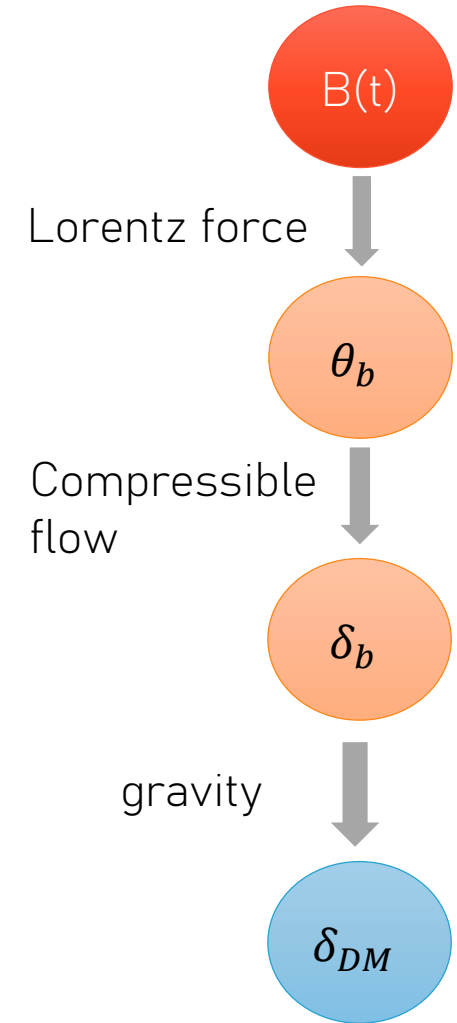
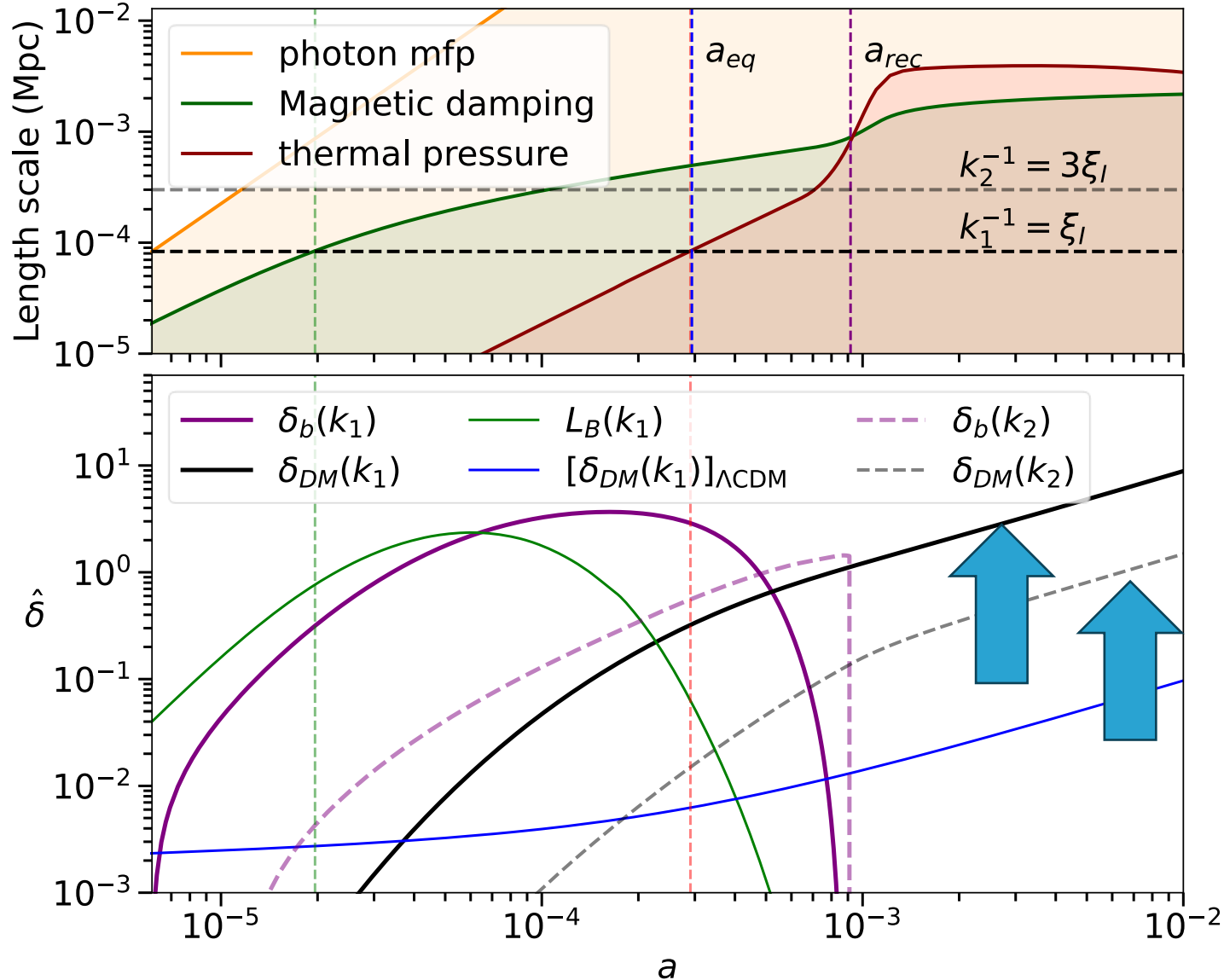
BARYON PERTURBATIONS DAMPED BY TURBULENCE AT RECOMBINATION

$B_I = 5 \text{ nG}$



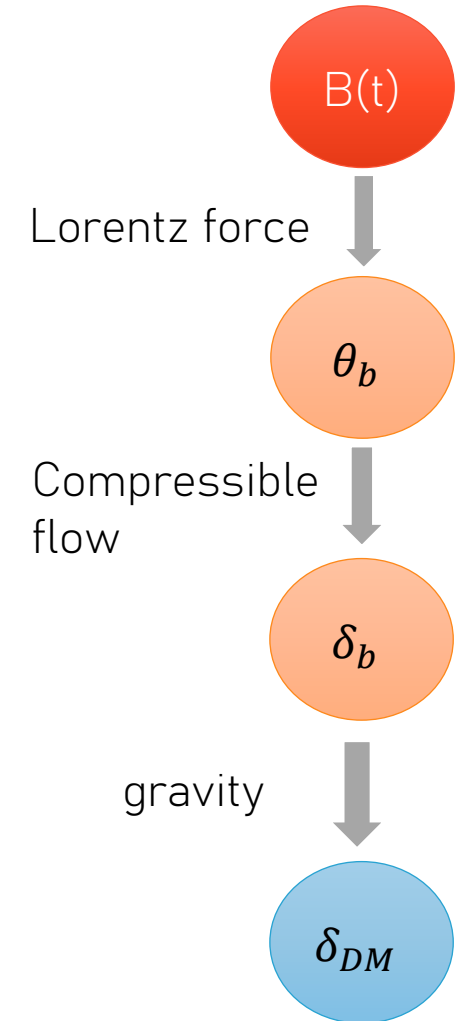
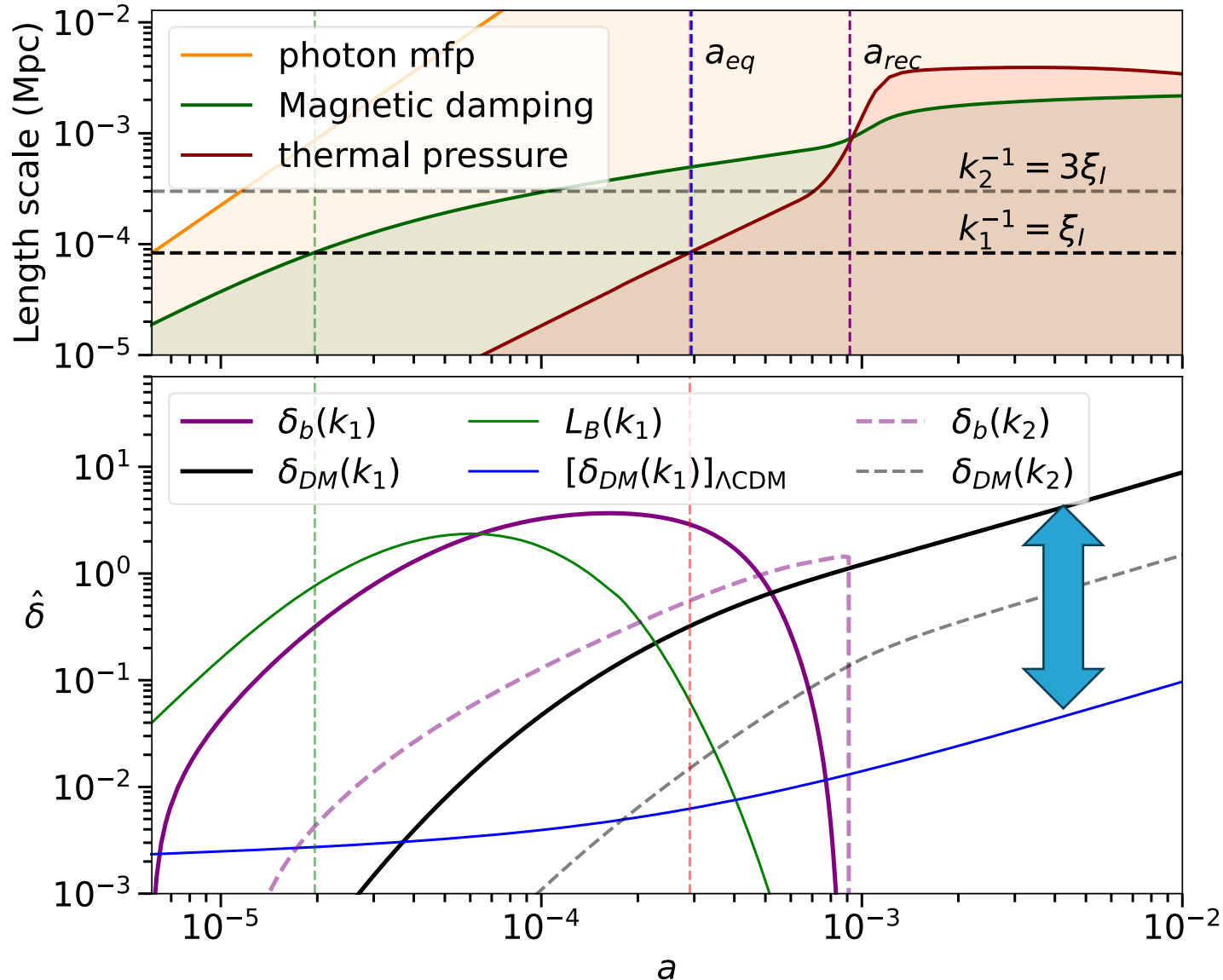
DARK MATTER PERTURBATIONS CONTINUES TO GROW!

$B_I = 5 \text{ nG}$

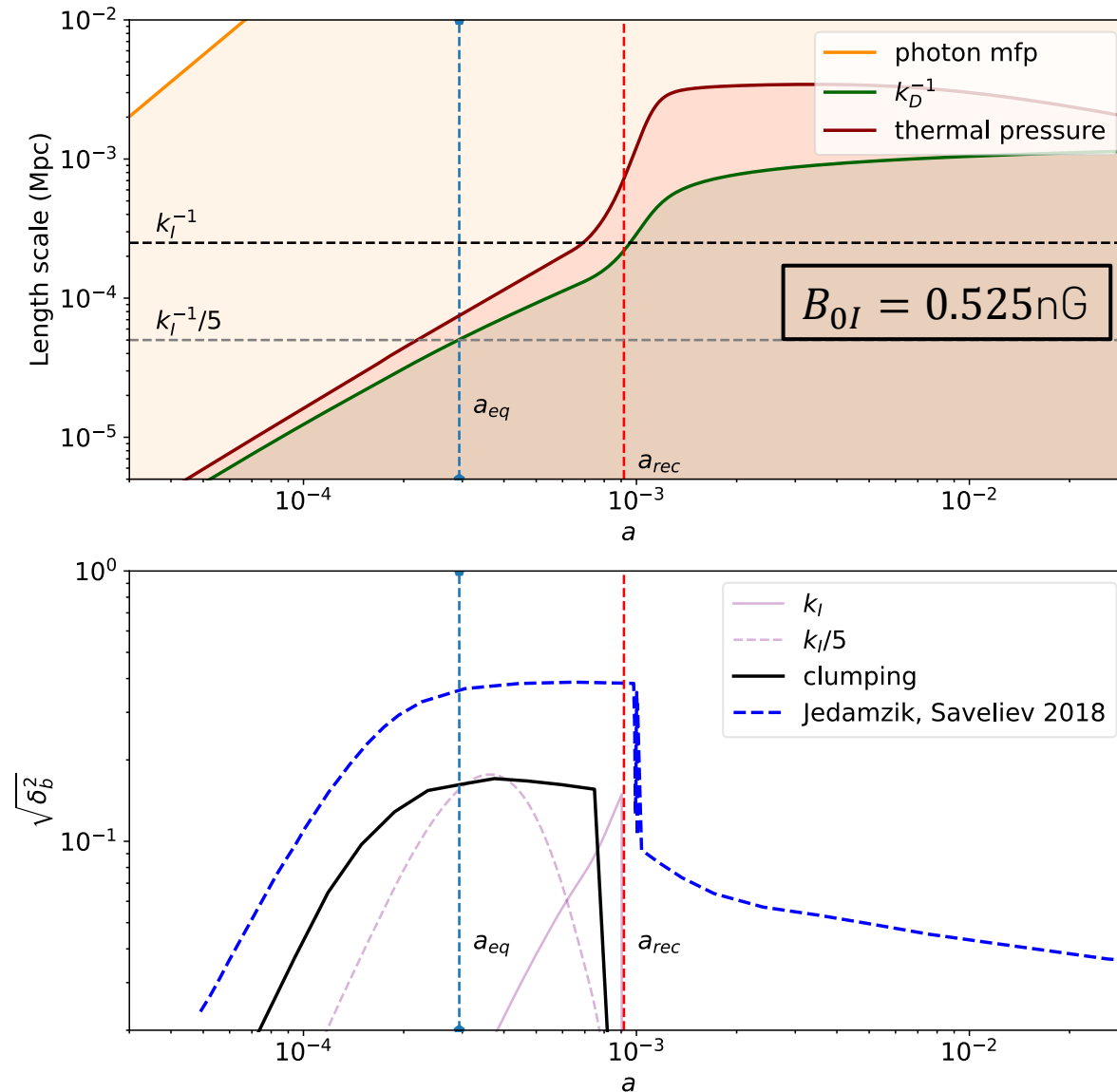


DARK MATTER PERTURBATIONS ENHANCED BY ORDERS OF MAGNITUDE COMPARED TO Λ CDM

$B_I = 5 \text{ nG}$

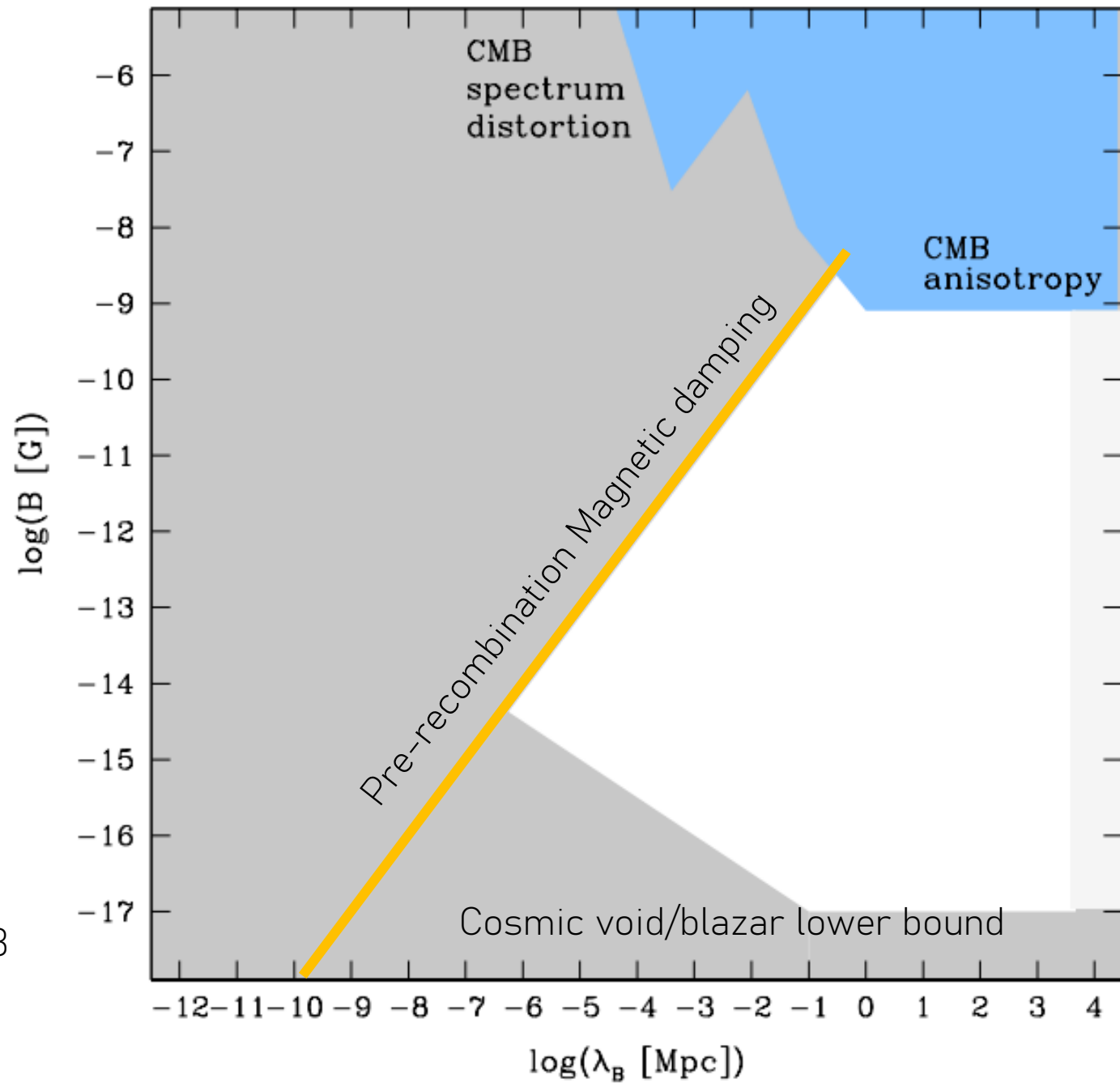


COMPARING WITH SIMULATIONS: ANALYTICAL NOT THAT BAD

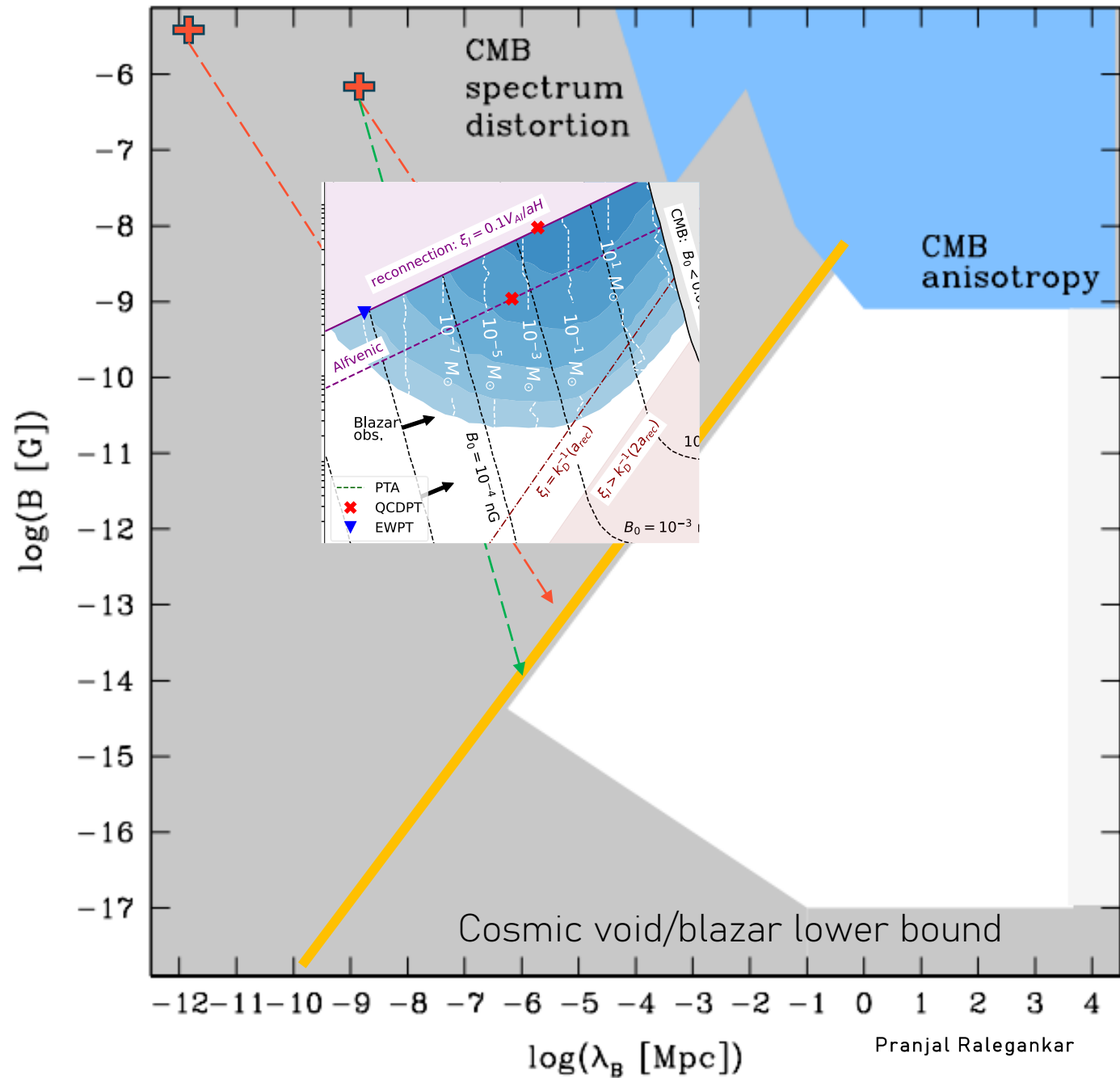


CONSTRAINTS ON PMF

Durrer and Neronov 2013

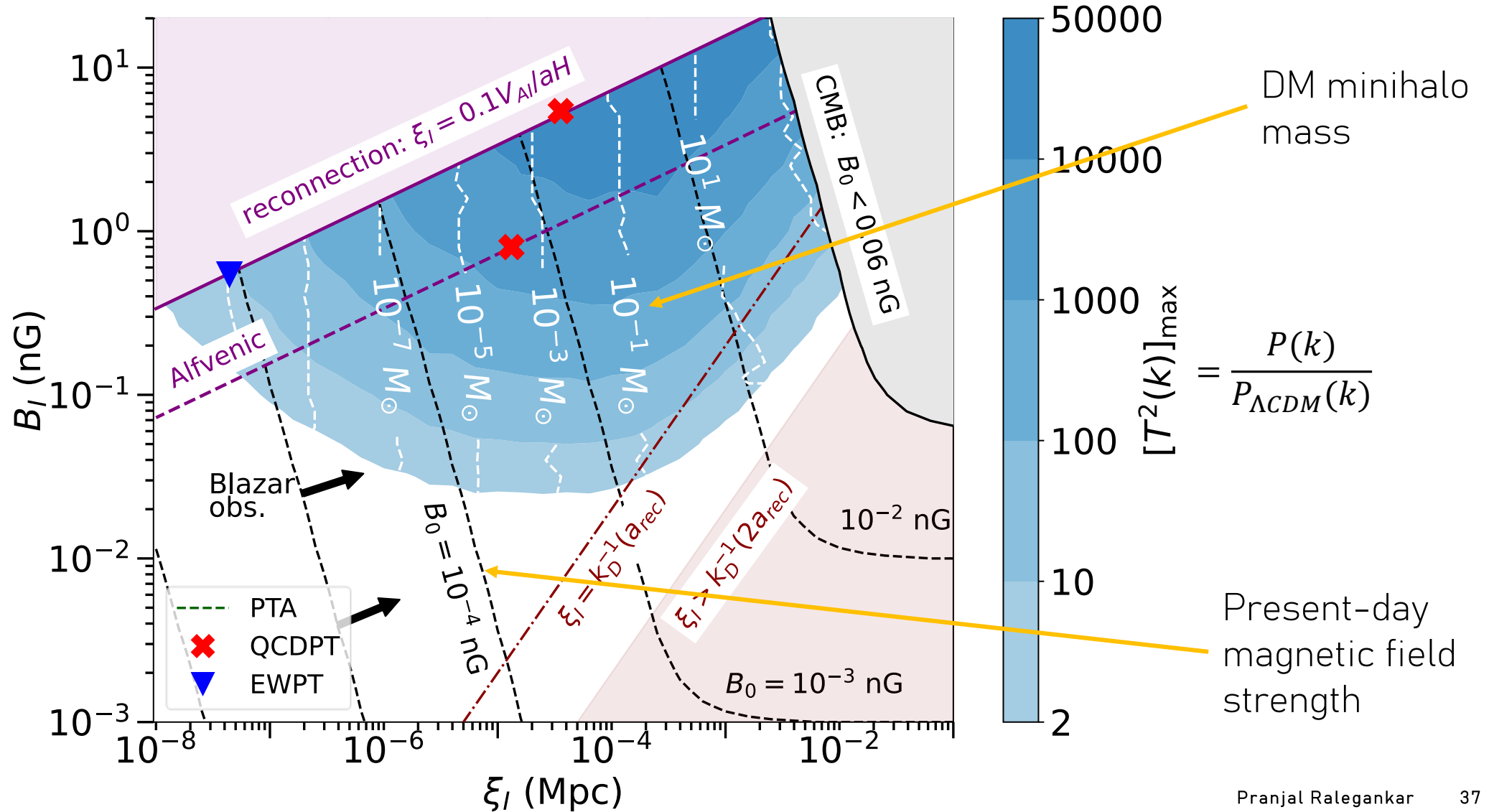


RELEVANCE OF DARK MATTER MINIHALO GENERATION



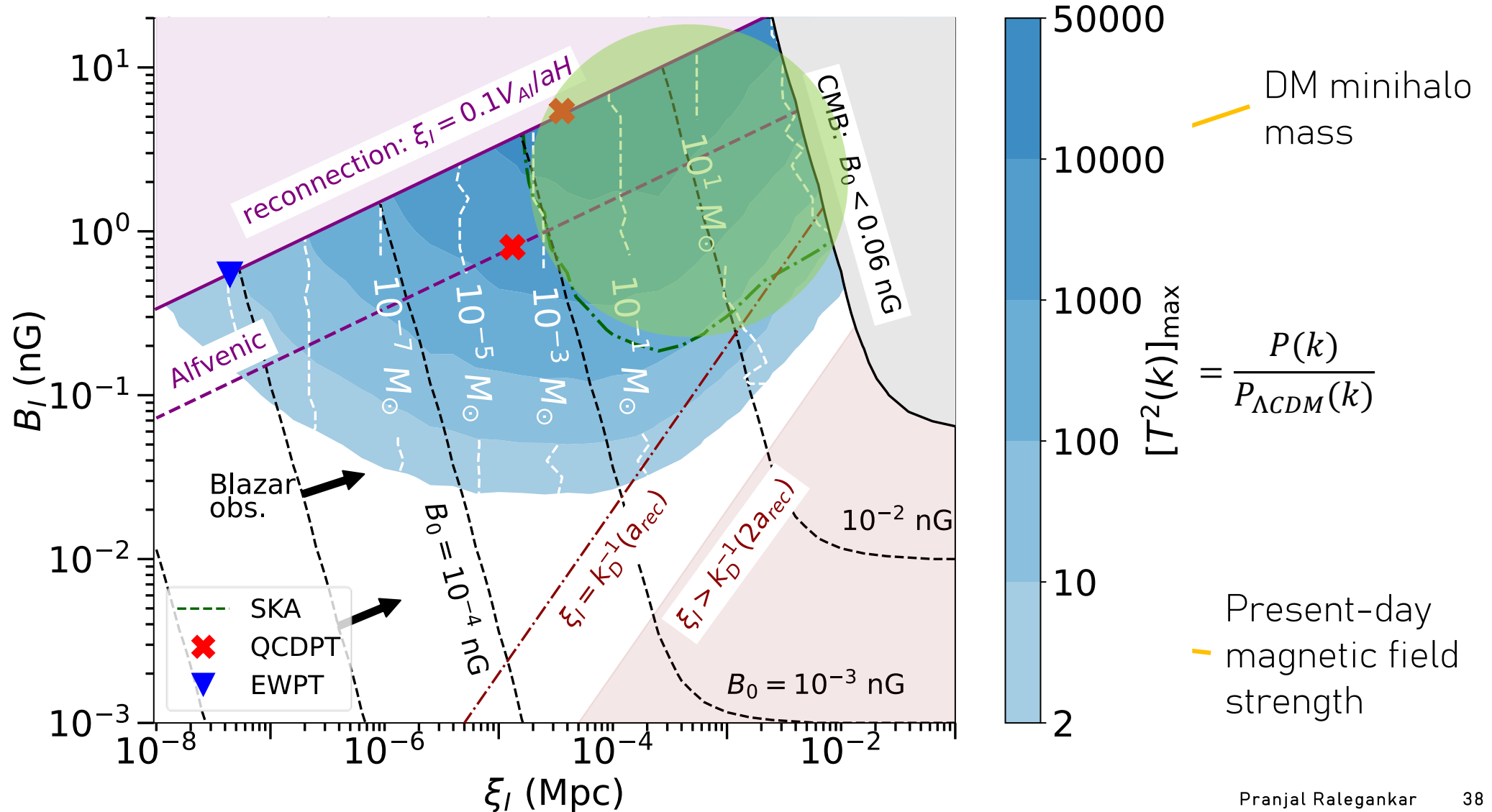
PARAMETER SPACE WITH ENHANCED POWER ON SMALL SCALES

Subscript I refers to the time at the beginning of laminar flow regime



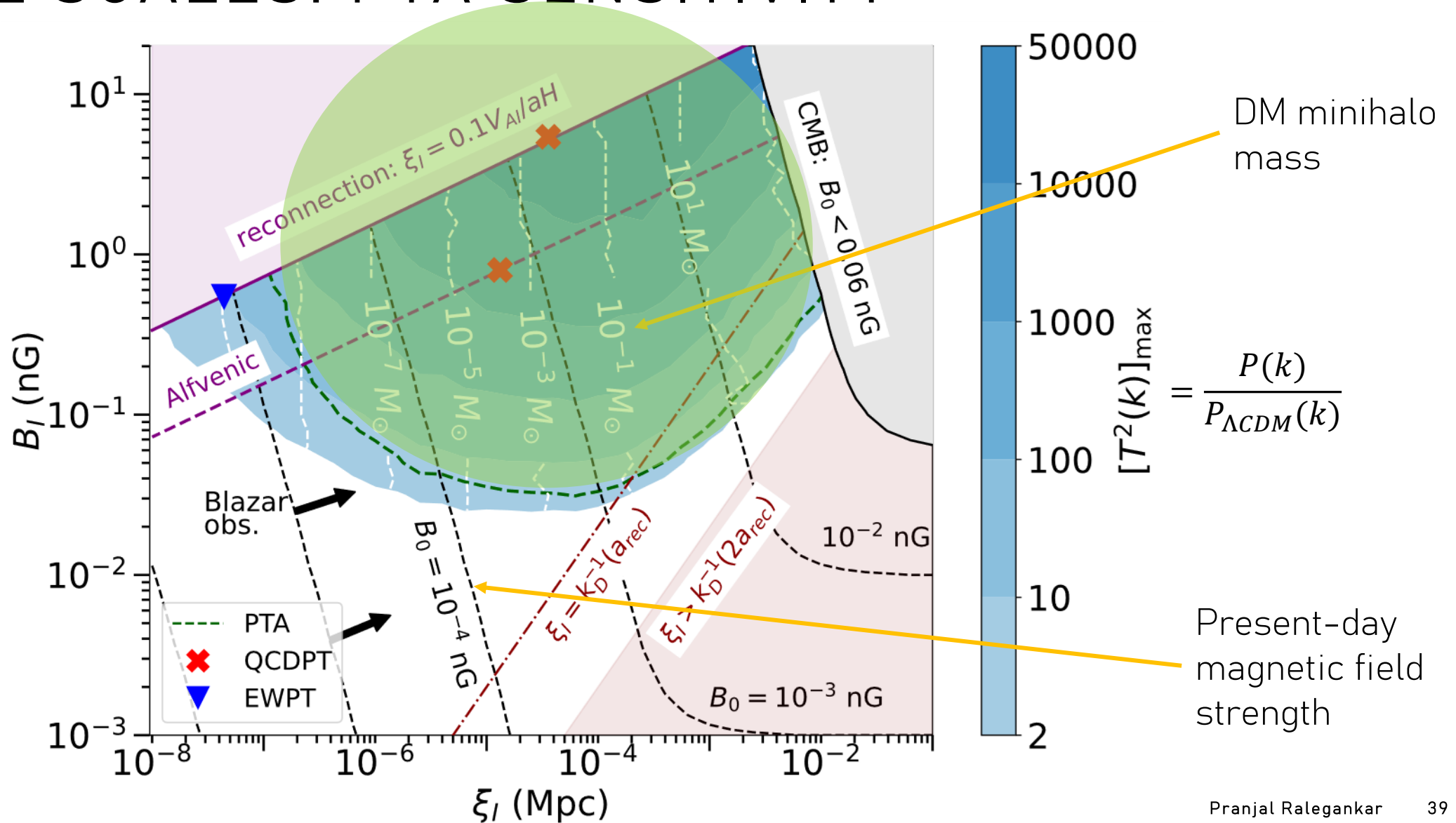
PARAMETER SPACE WITH ENHANCED POWER ON SMALL SCALES: THEIA SKA SENSITIVITY

Subscript I refers to the time at the beginning of laminar flow regime

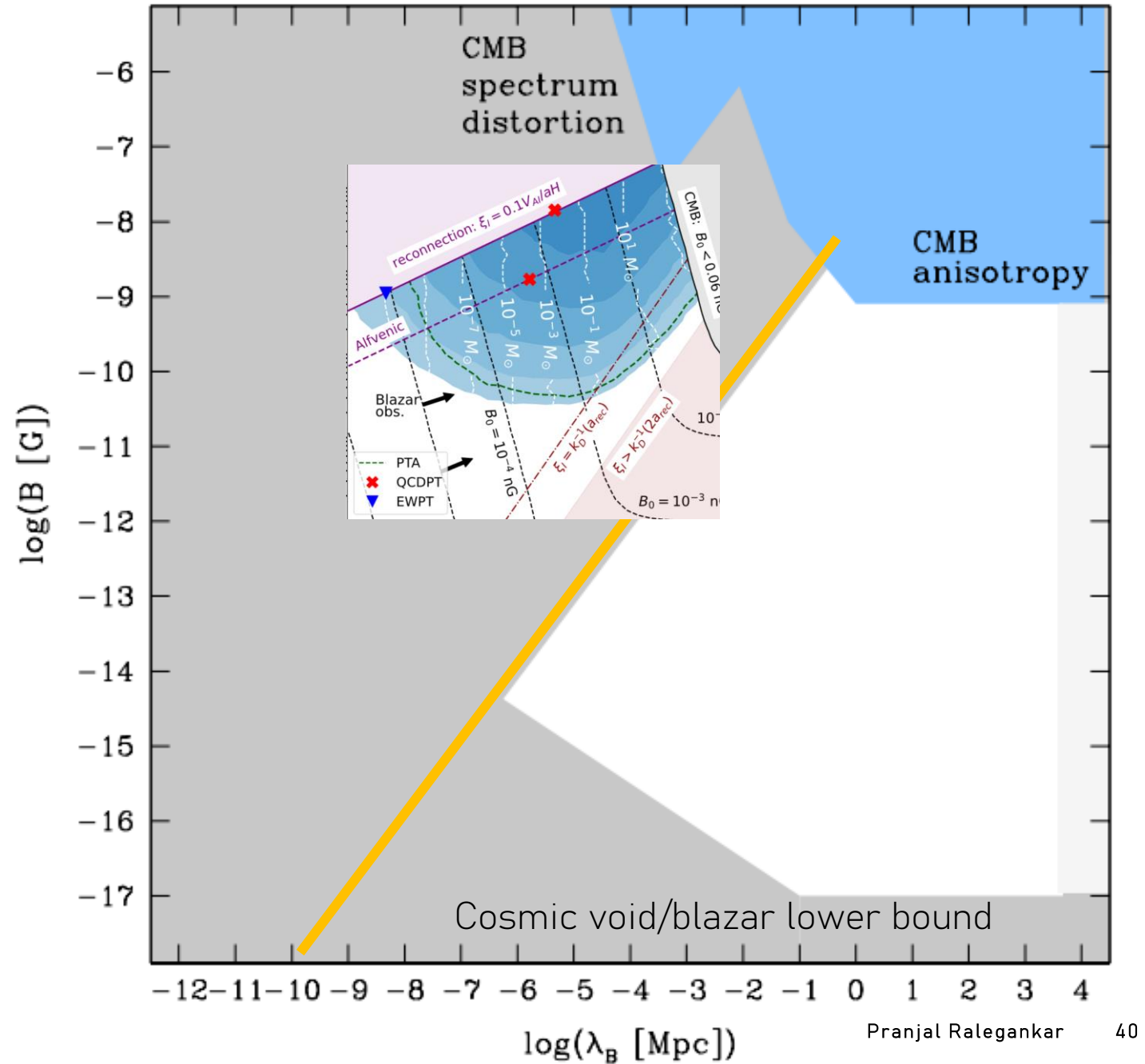


PARAMETER SPACE WITH ENHANCED POWER ON SMALL SCALES: PTA SENSITIVITY

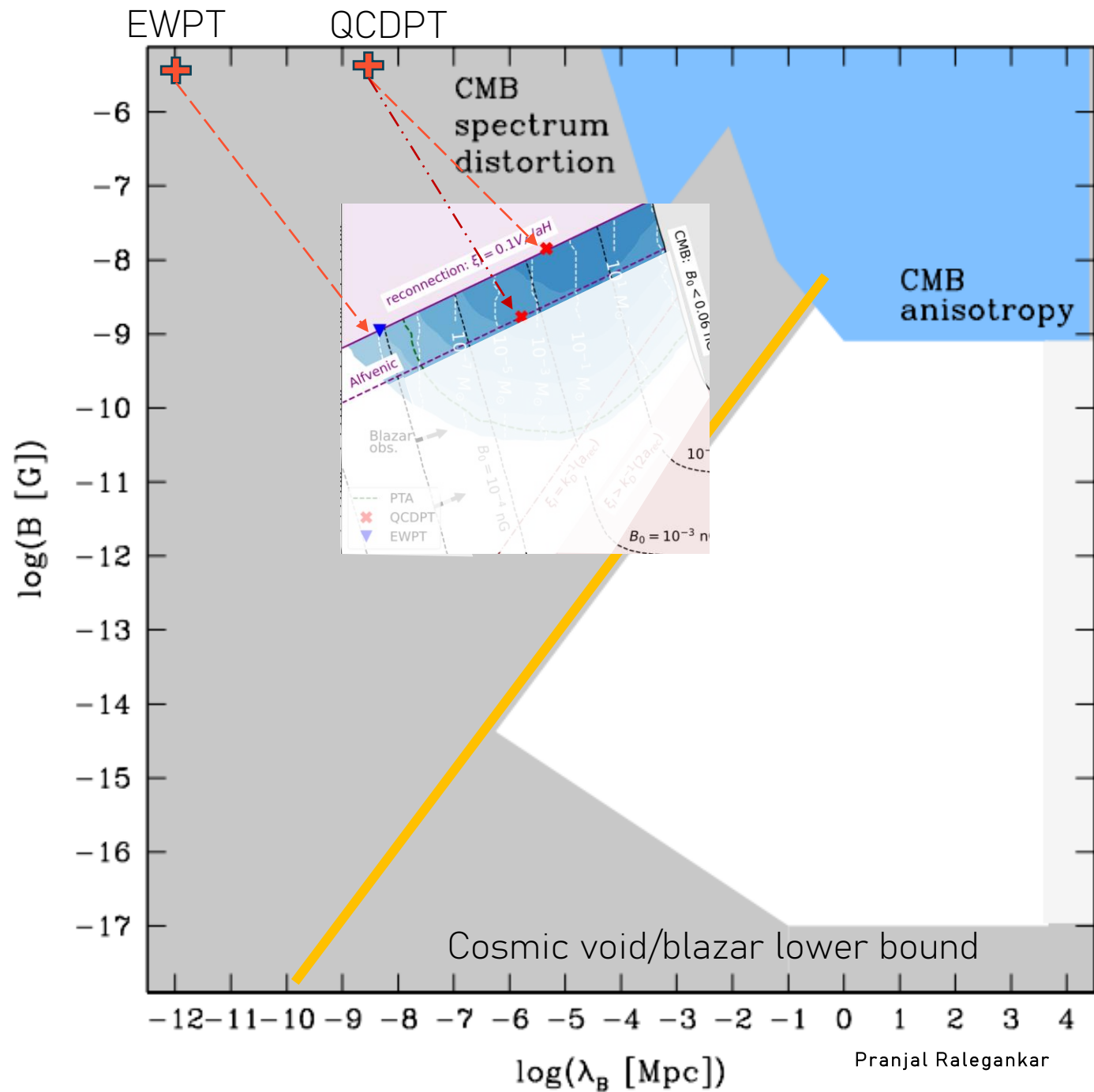
Subscript I refers to the time at the beginning of laminar flow regime



MINIHALOS FROM CAUSALLY GENERATED PMFS

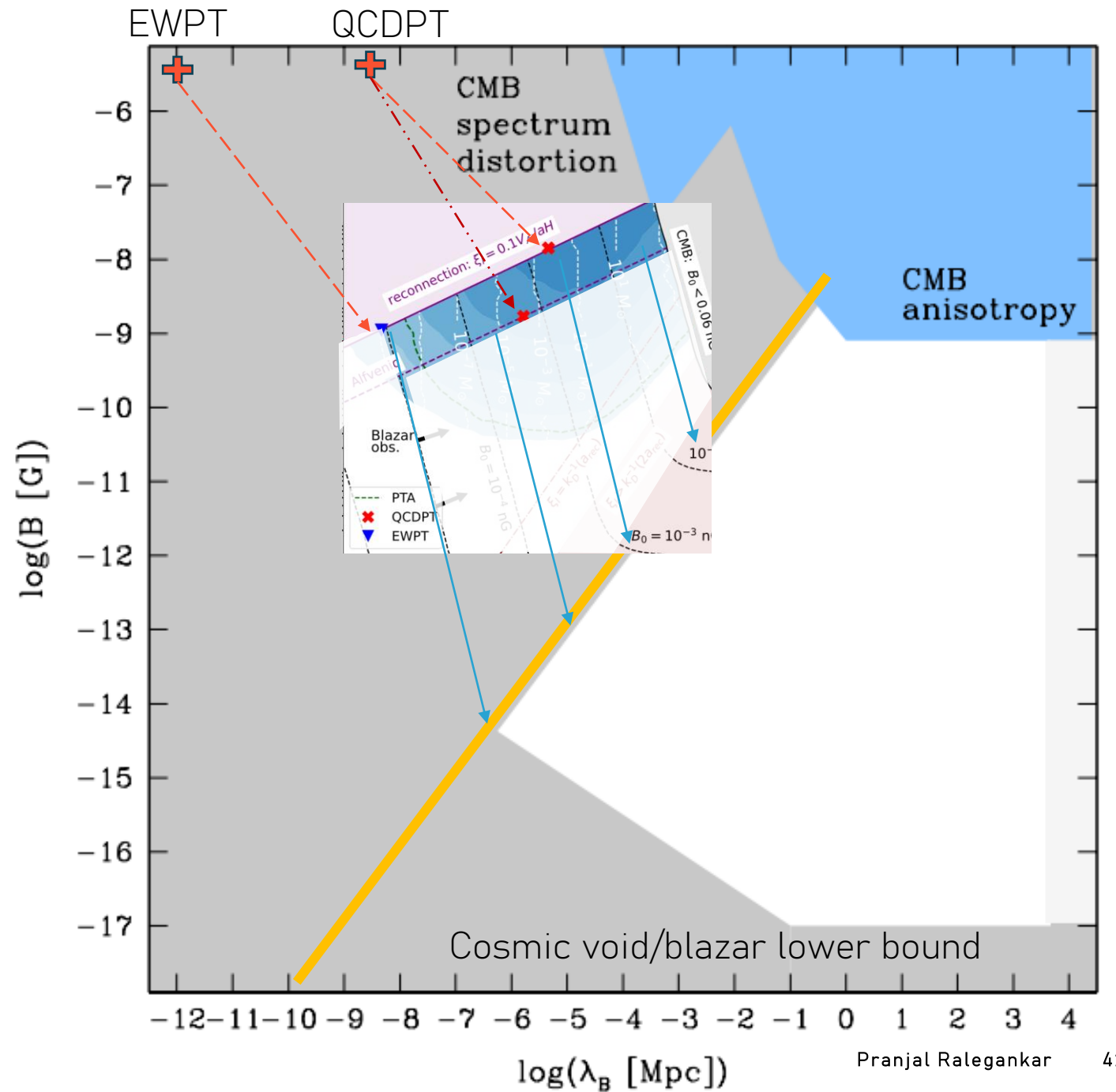


MINIHALOS FROM CAUSALLY GENERATED PMFS



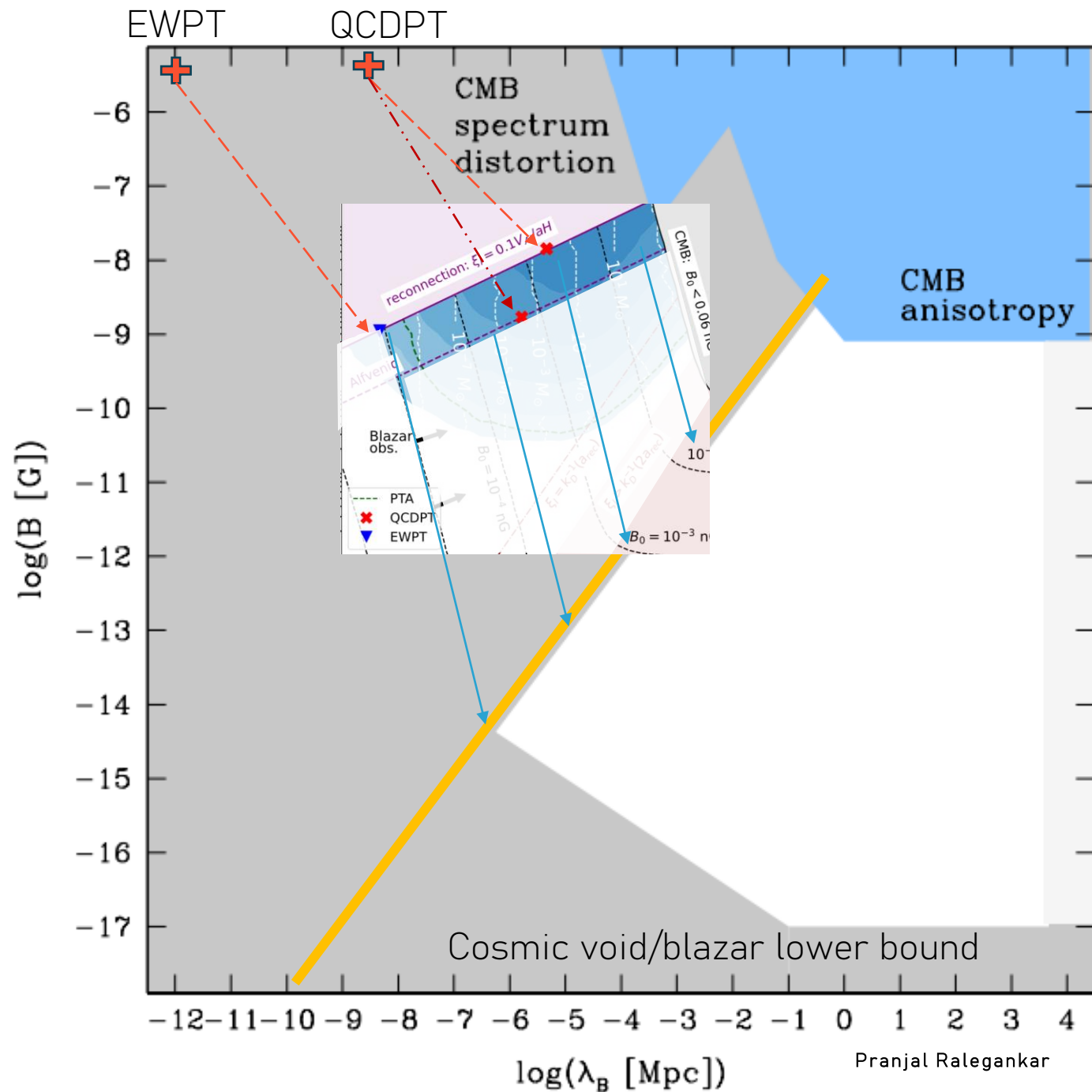
PMFS TO EXPLAIN COSMIC VOID OBSERVATIONS

Assuming Batchelor spectrum!



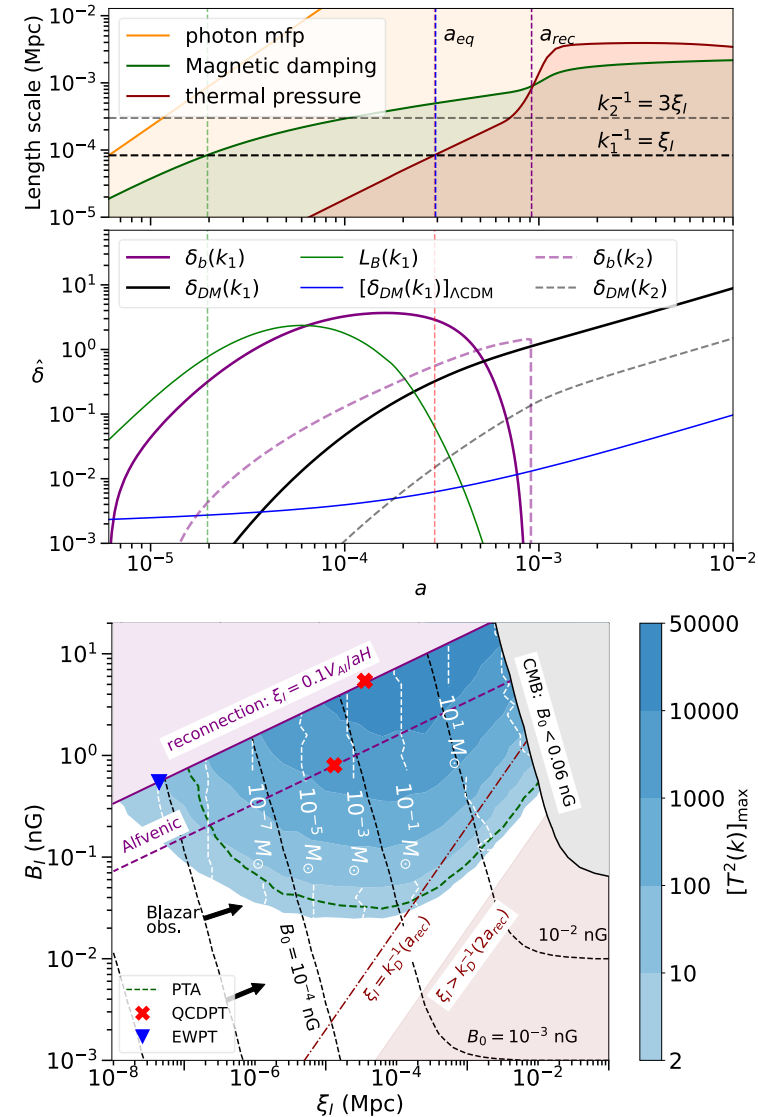
UNIVERSE MAYBE FILLED WITH DARK MATTER MINIHALOS!!

Assuming Batchelor spectrum!



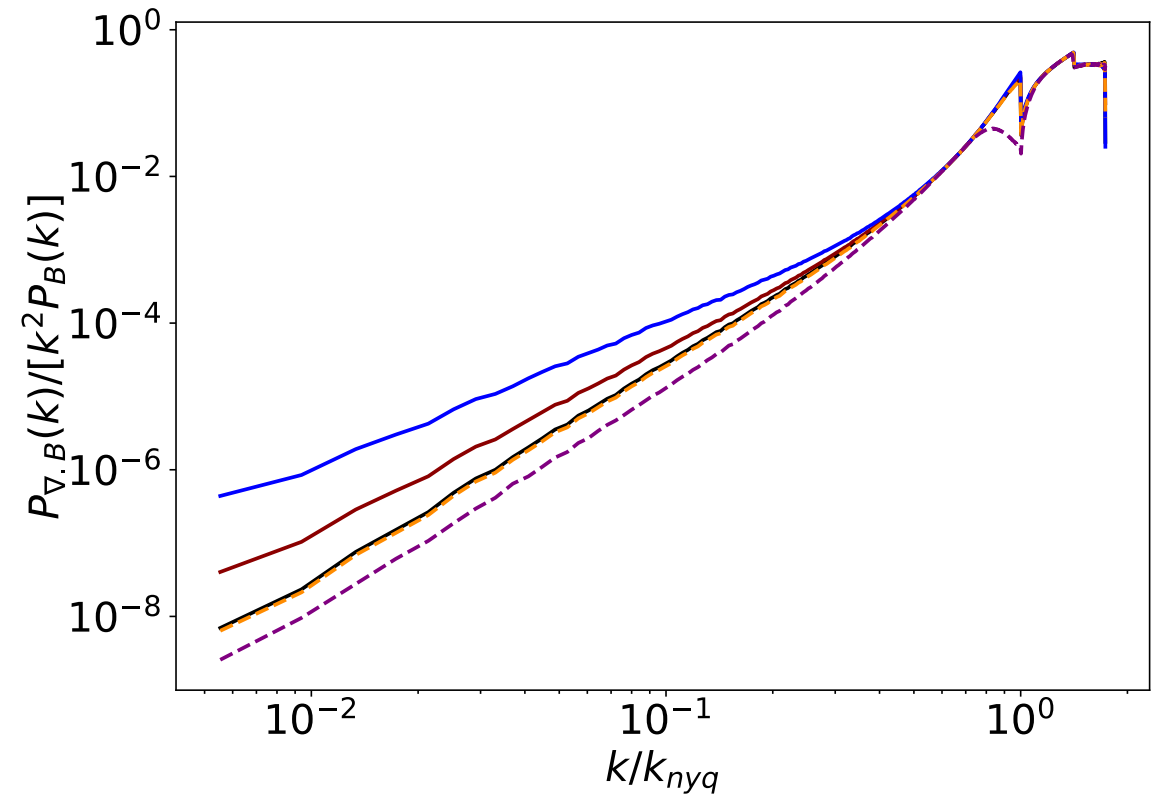
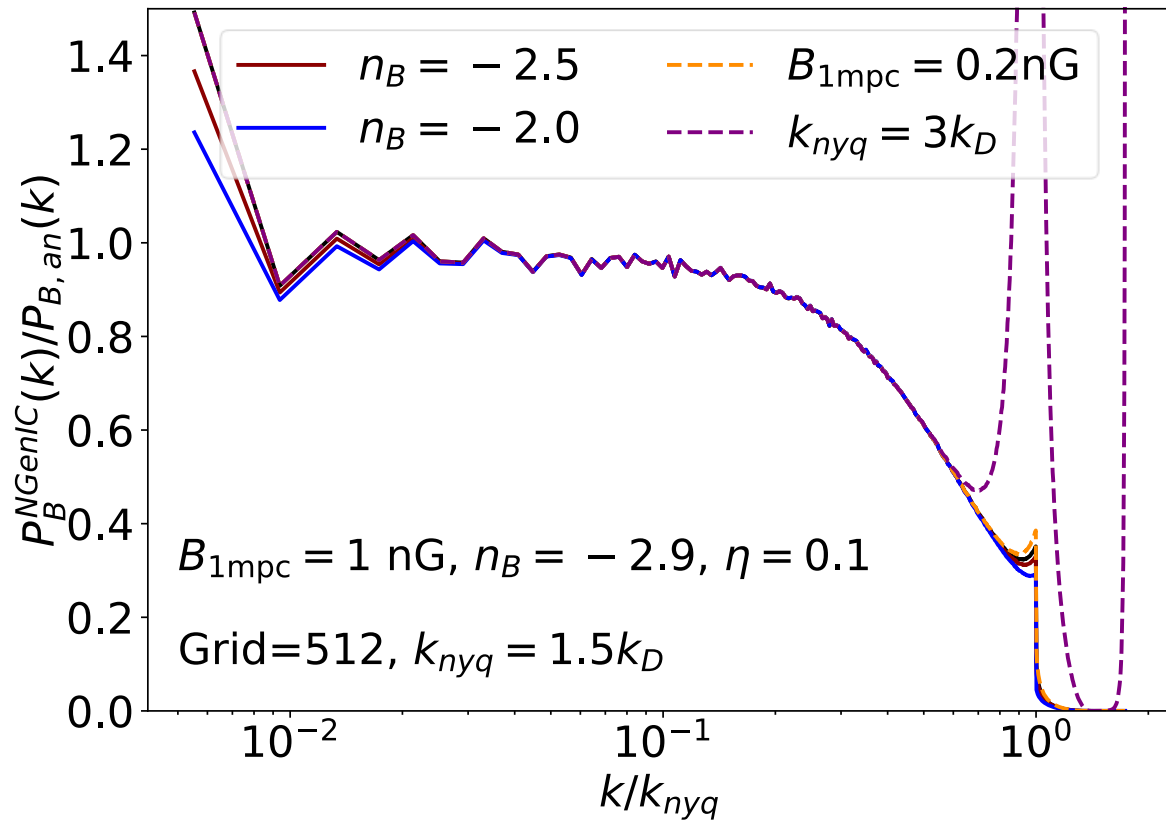
SUMMARY AND CONCLUDING REMARKS

- Magnetic fields can enhance power dark matter power spectrum below magnetic Jeans scale.
- PTA/GAIA detection of DM minihalos can provide best probe of primordial magnetic fields
- Results are qualitative: Need MHD simulations to get accurate quantitative answers.
- Ironic: how invisible dark matter can help look for visible entity: magnetic fields

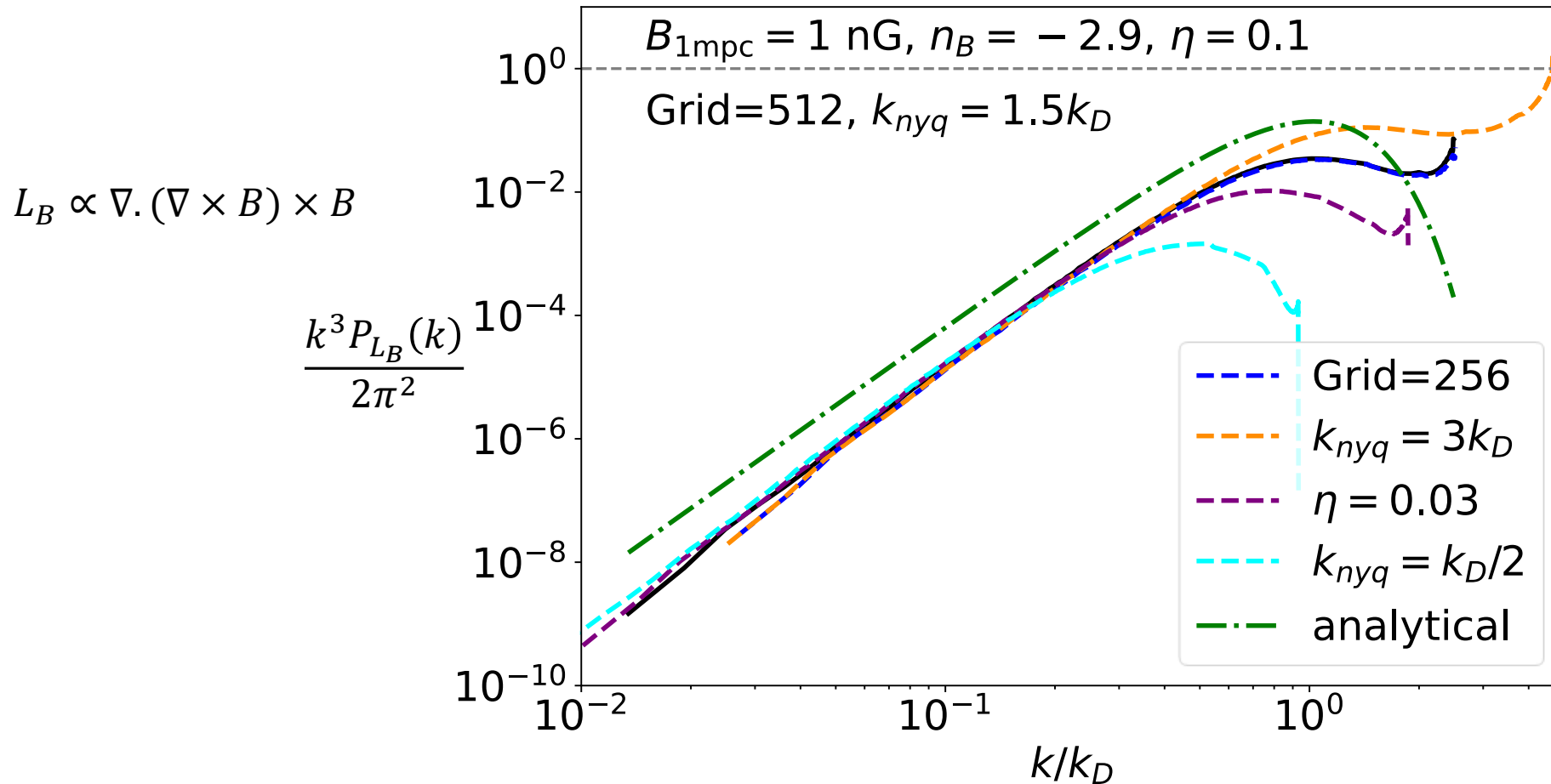


PROBLEM WITH LORENTZ FORCE IN MY LATTICE

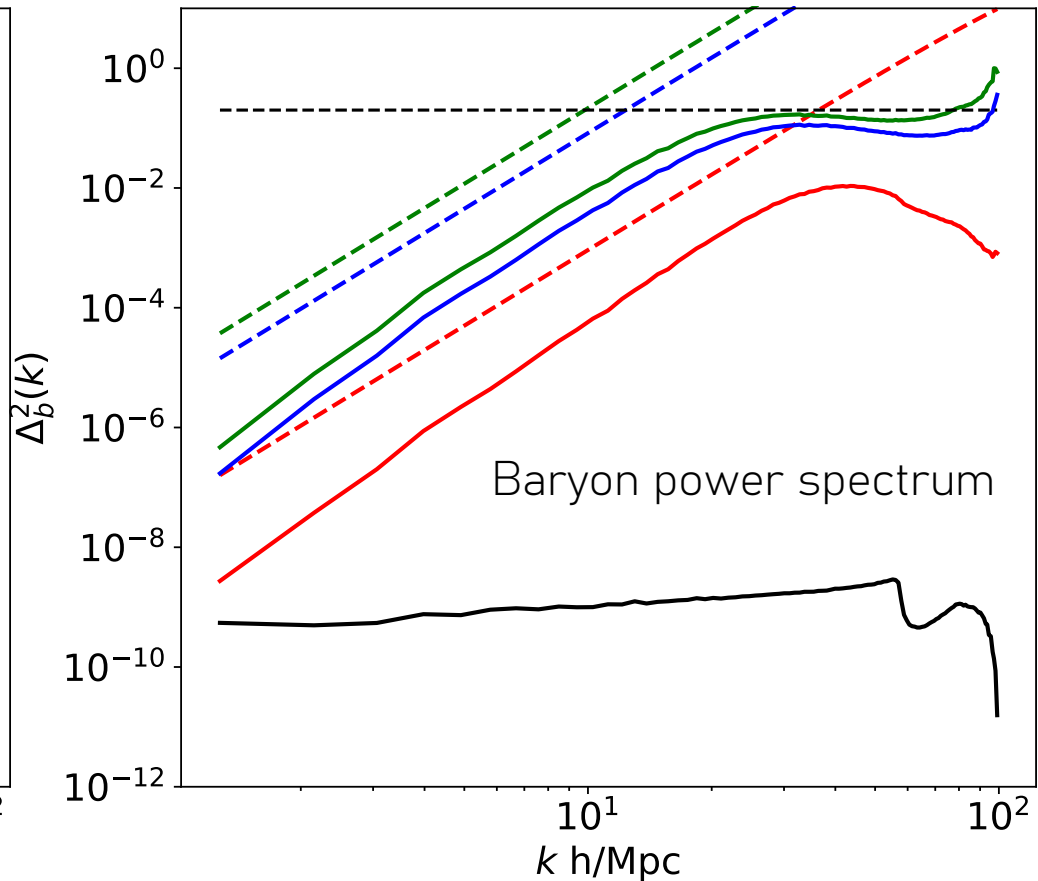
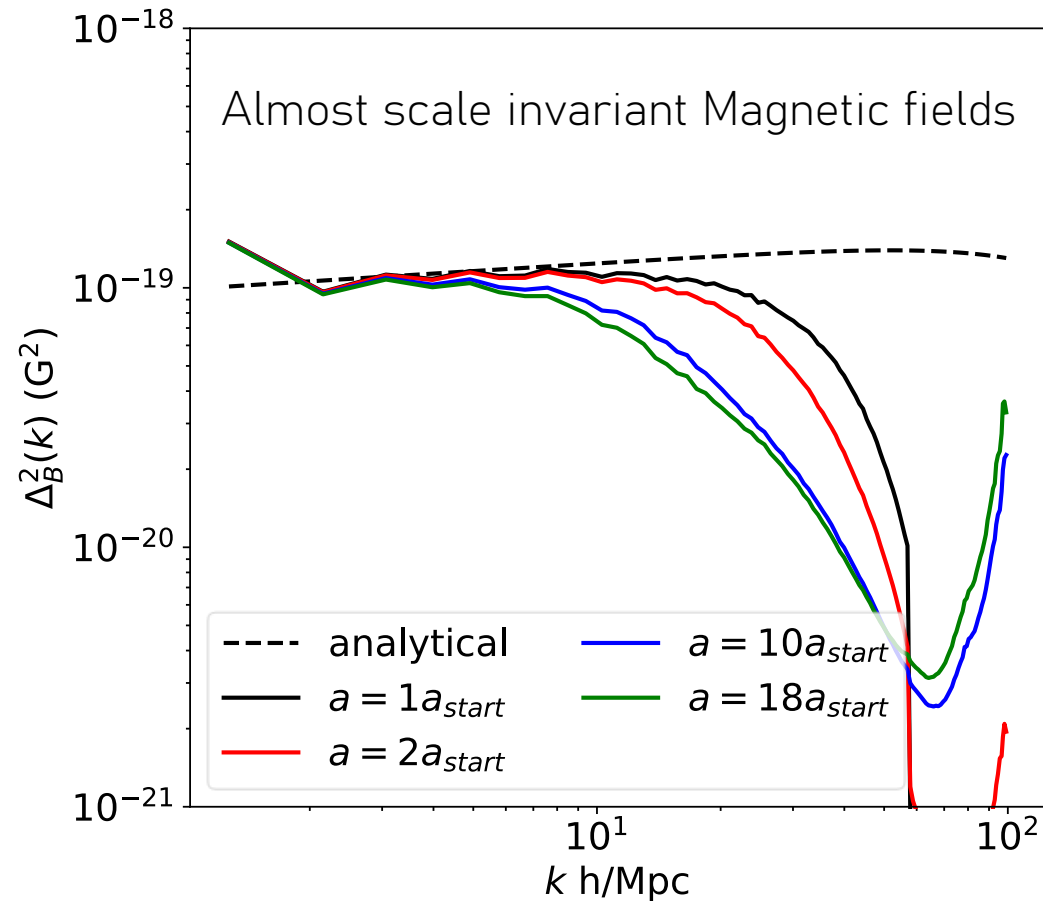
INITIALIZING STOCHASTIC PMFS ON LATTICE



LORENTZ FORCE POWER SPECTRUM DOESN'T AGREE WITH THEORY



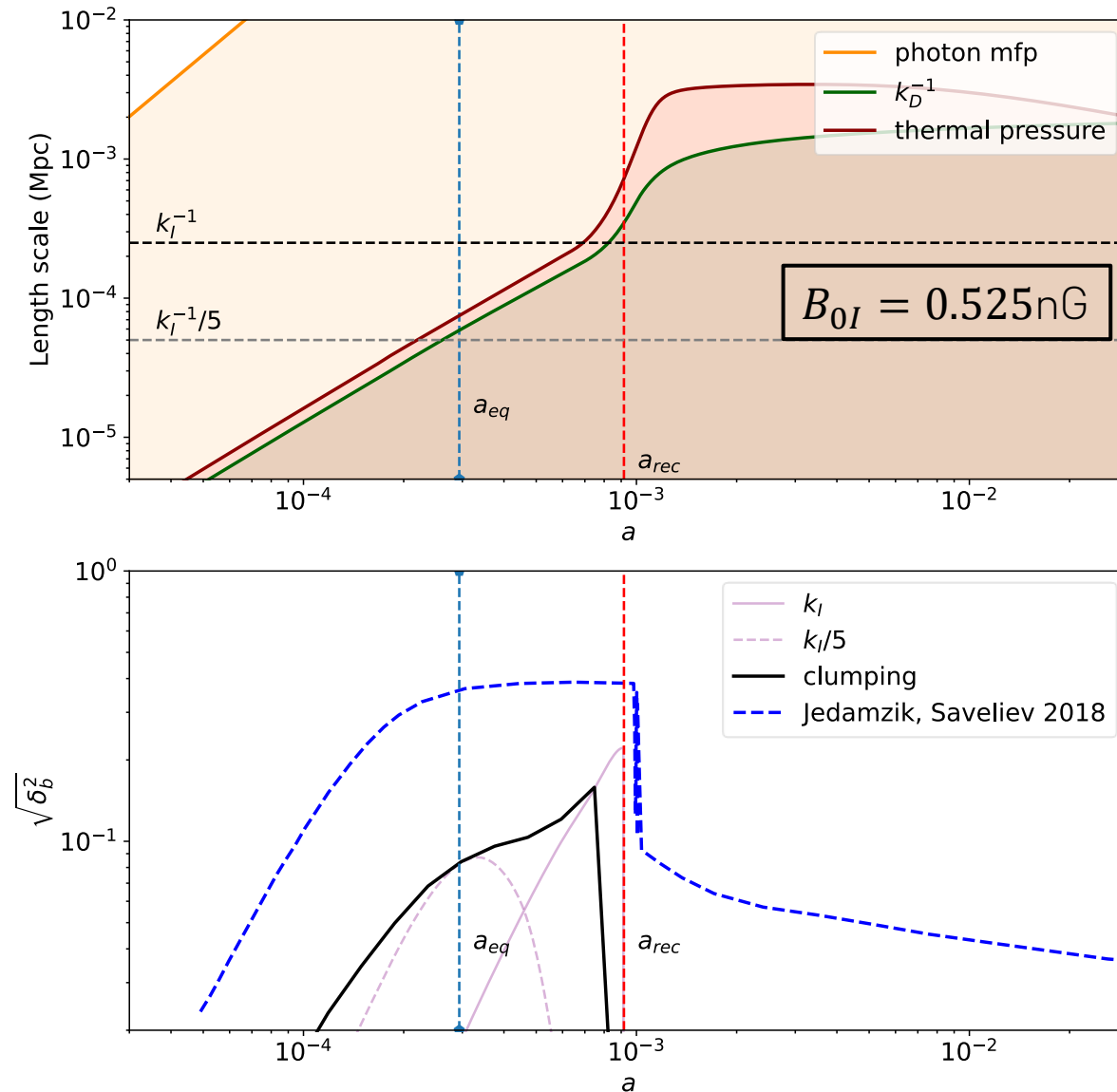
THE SUPPRESSION OF POWER IS ALSO SEEN IN AREPO (PRELIMINARY!!)



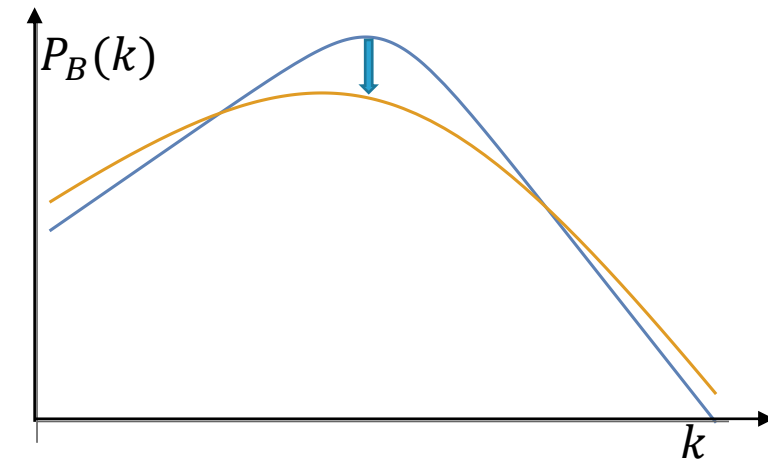
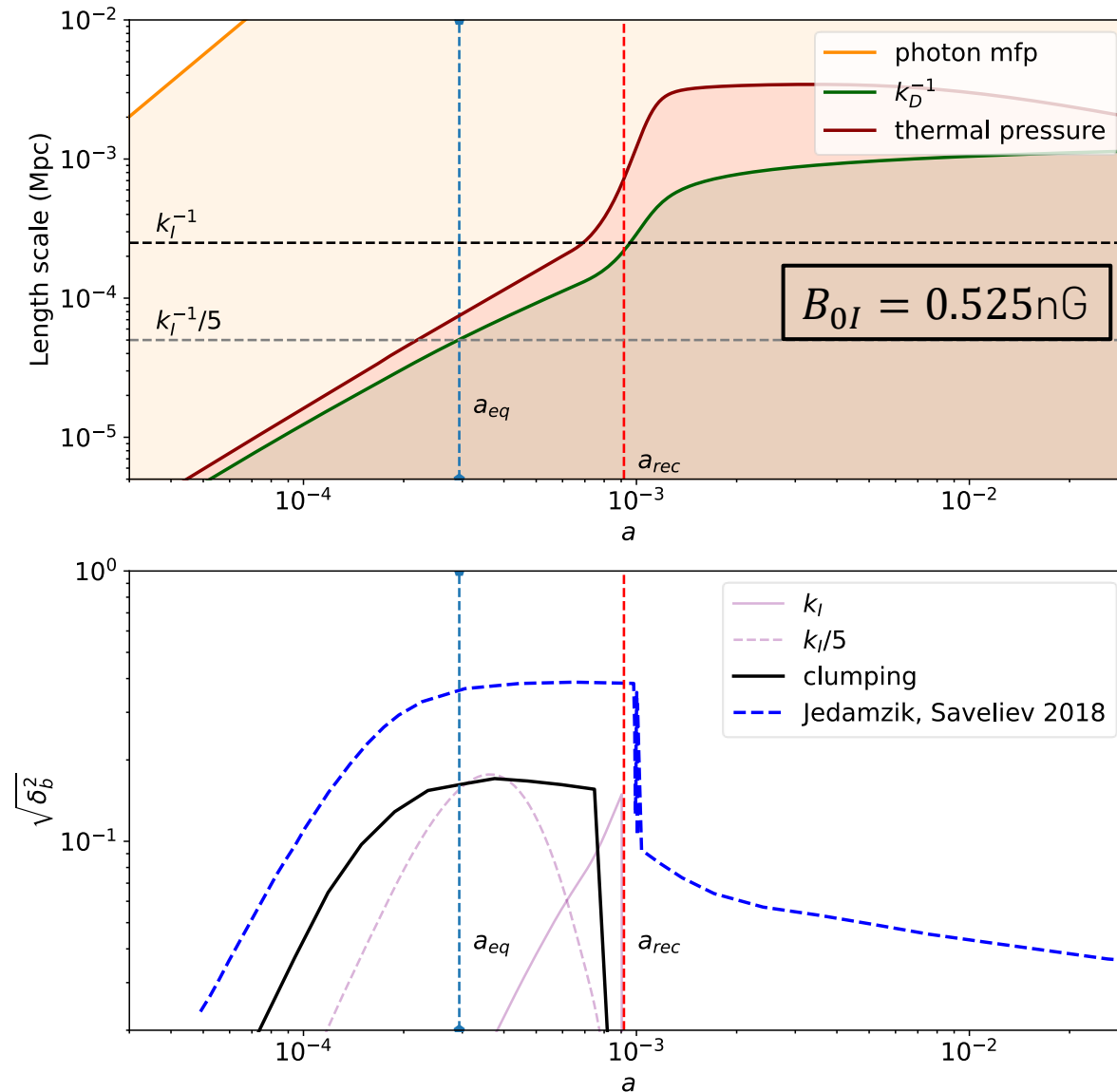
BACKUP SLIDES

COMPARING WITH FULL MHD SIMULATIONS

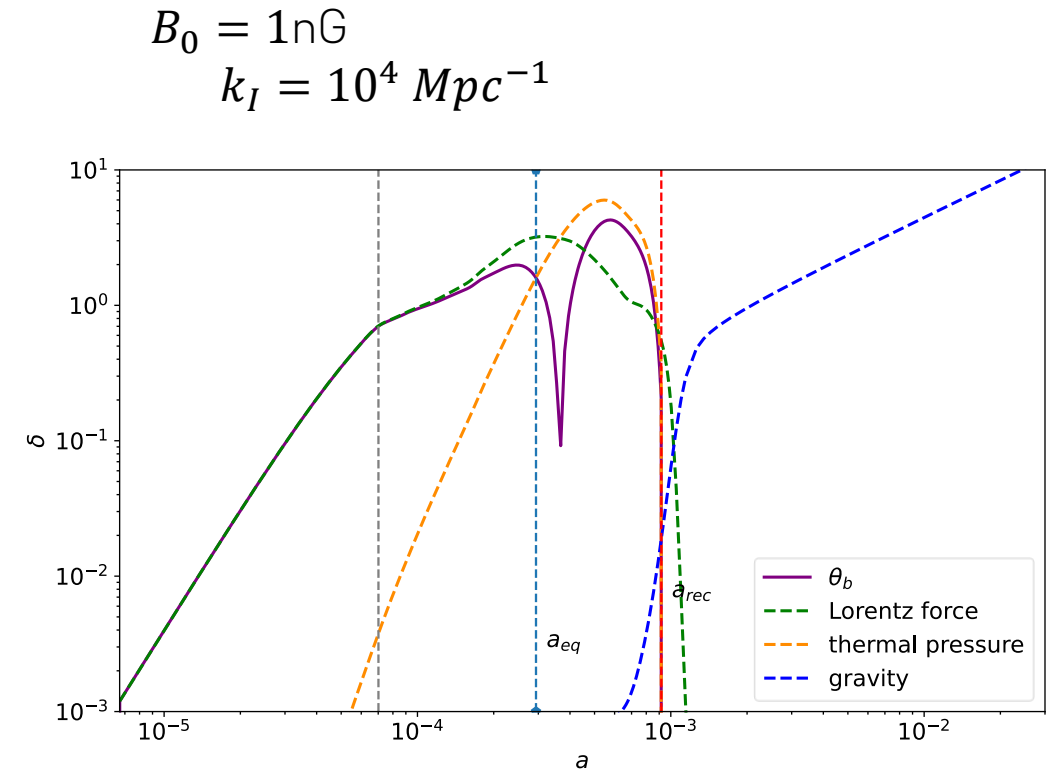
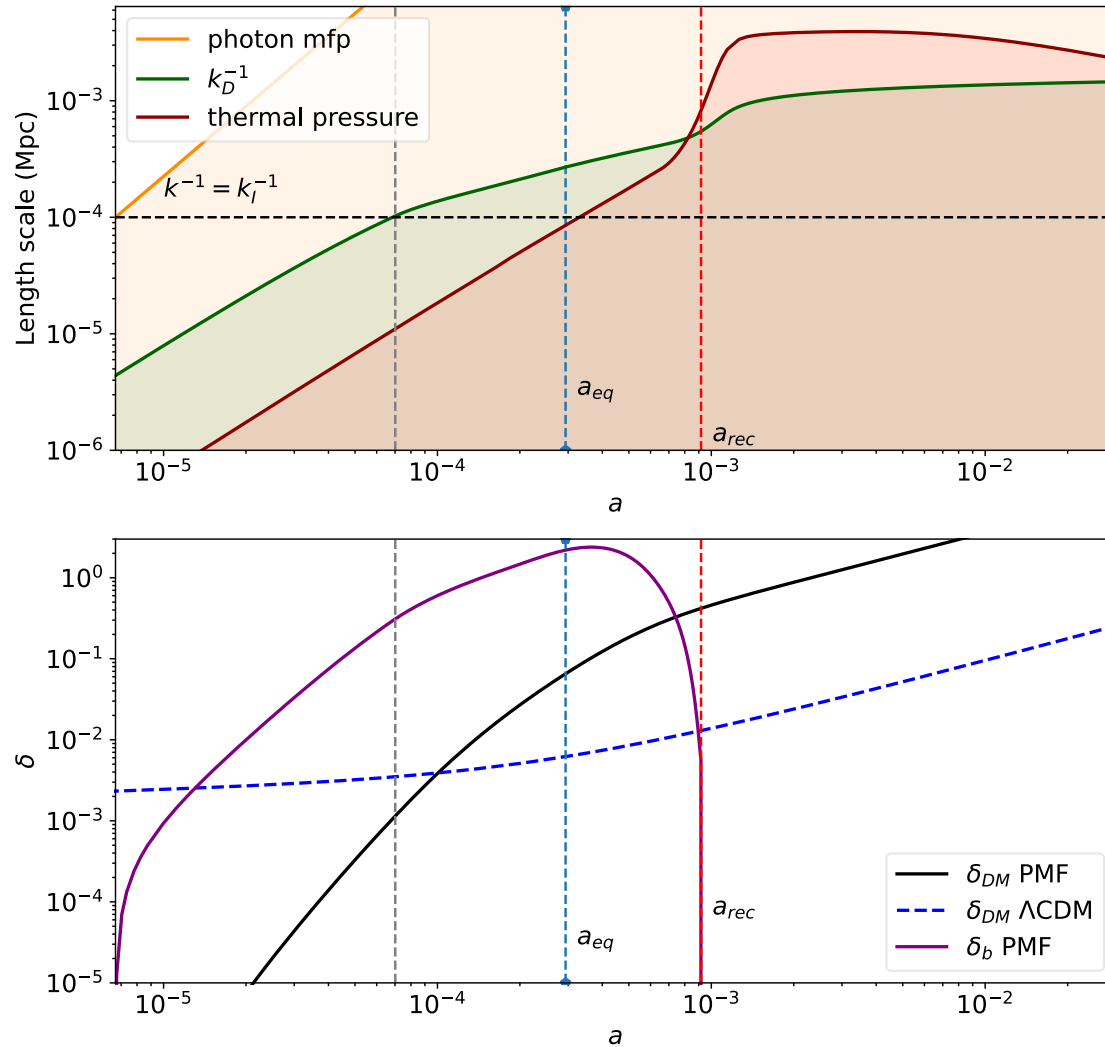
COMPARING WITH SIMULATIONS: SENSITIVE TO INITIAL POWER SPECTRUM



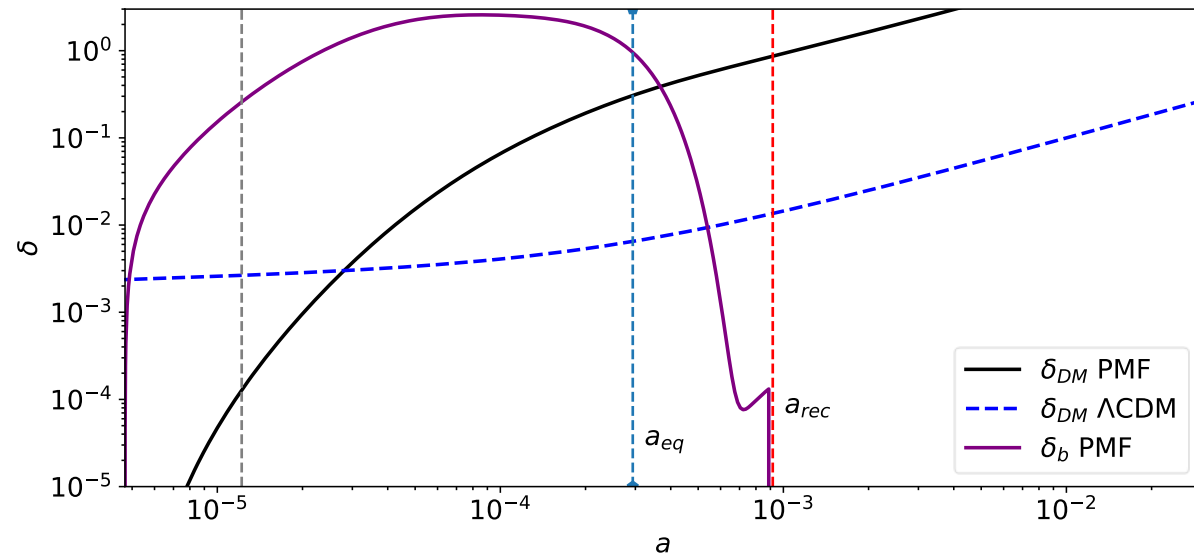
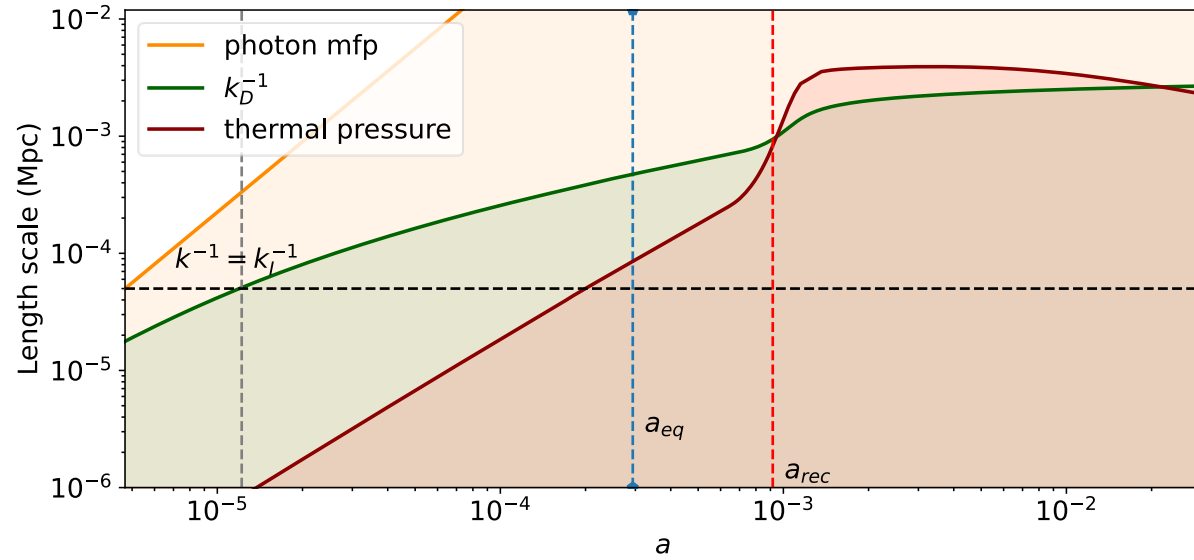
COMPARING WITH SIMULATIONS: SENSITIVE TO INITIAL POWER SPECTRUM



MORE PERTURBATION PLOTS



MORE PERTURBATION PLOTS



$$B_0 = 8 \text{ nG}$$

$$k_I = 10^4 \text{ Mpc}^{-1}$$

